

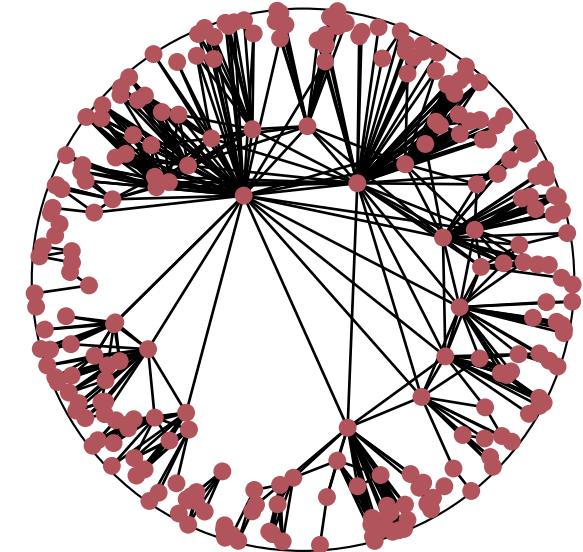
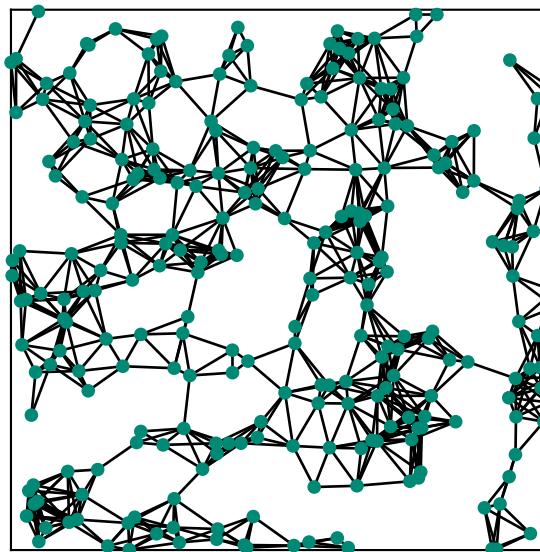
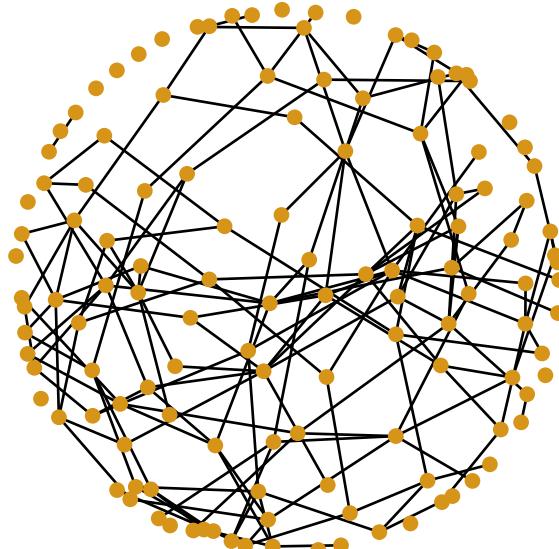
We Got You Covered

The Winning Solver from the PACE 2019 Implementation Challenge, Vertex Cover Track

IPEC'19 · September 11, 2019

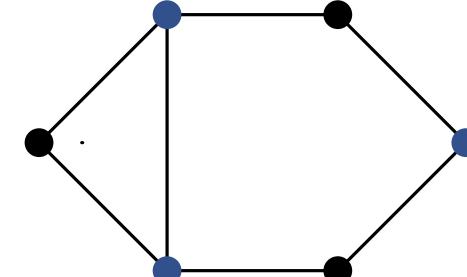
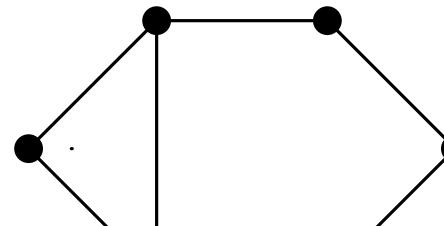
Demian Hespe, Sebastian Lamm, Christian Schulz, Darren Strash

INSTITUTE OF THEORETICAL INFORMATICS · ALGORITHMIC GROUP

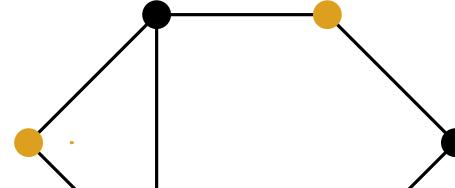


Vertex Cover and Complementary Problems

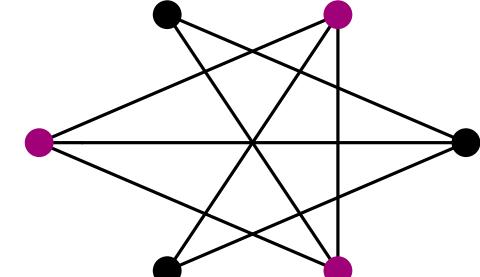
Input graph



Vertex cover



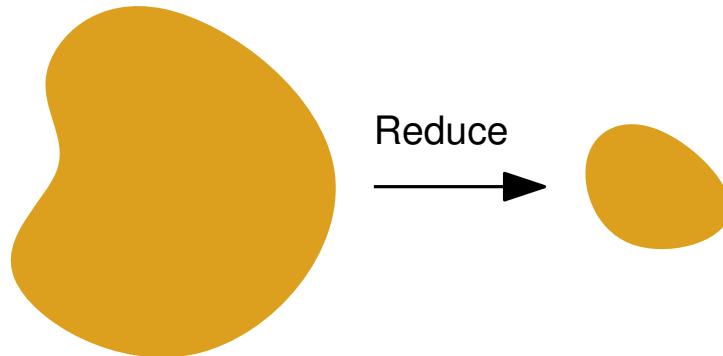
Independent Set



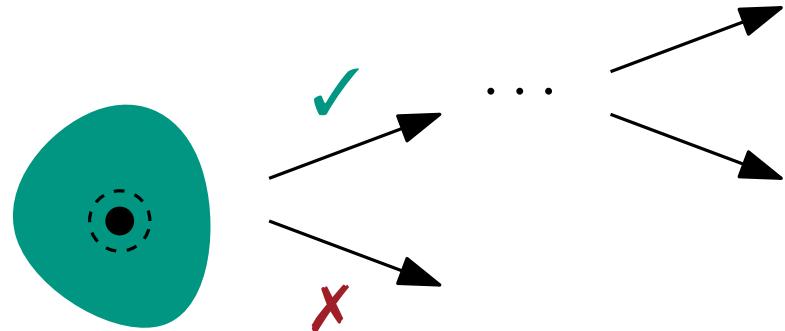
Clique

Techniques

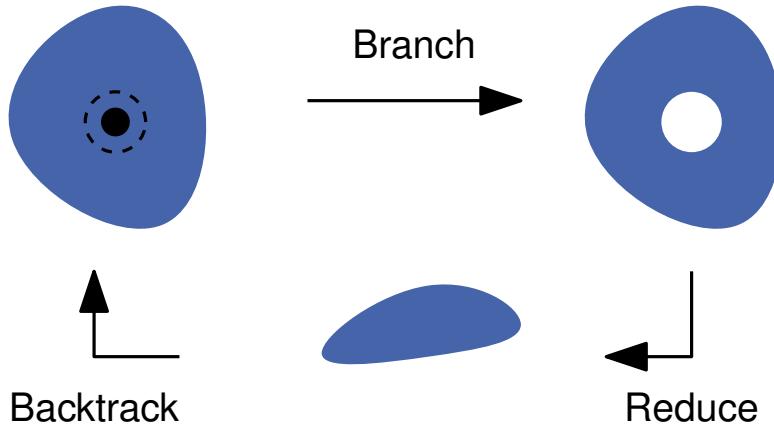
Kernelization



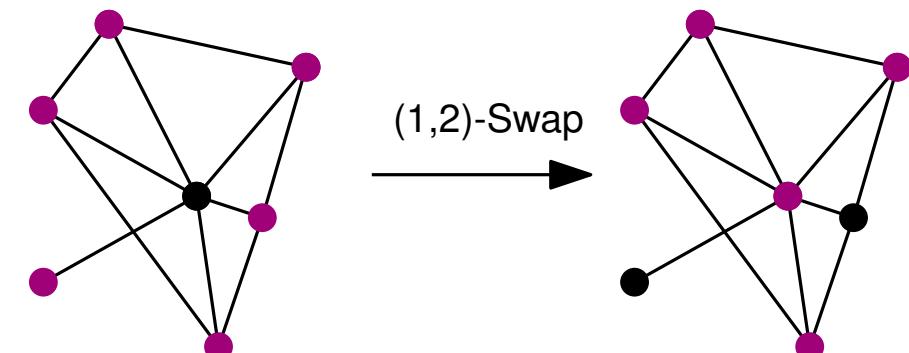
Branch-and-Bound



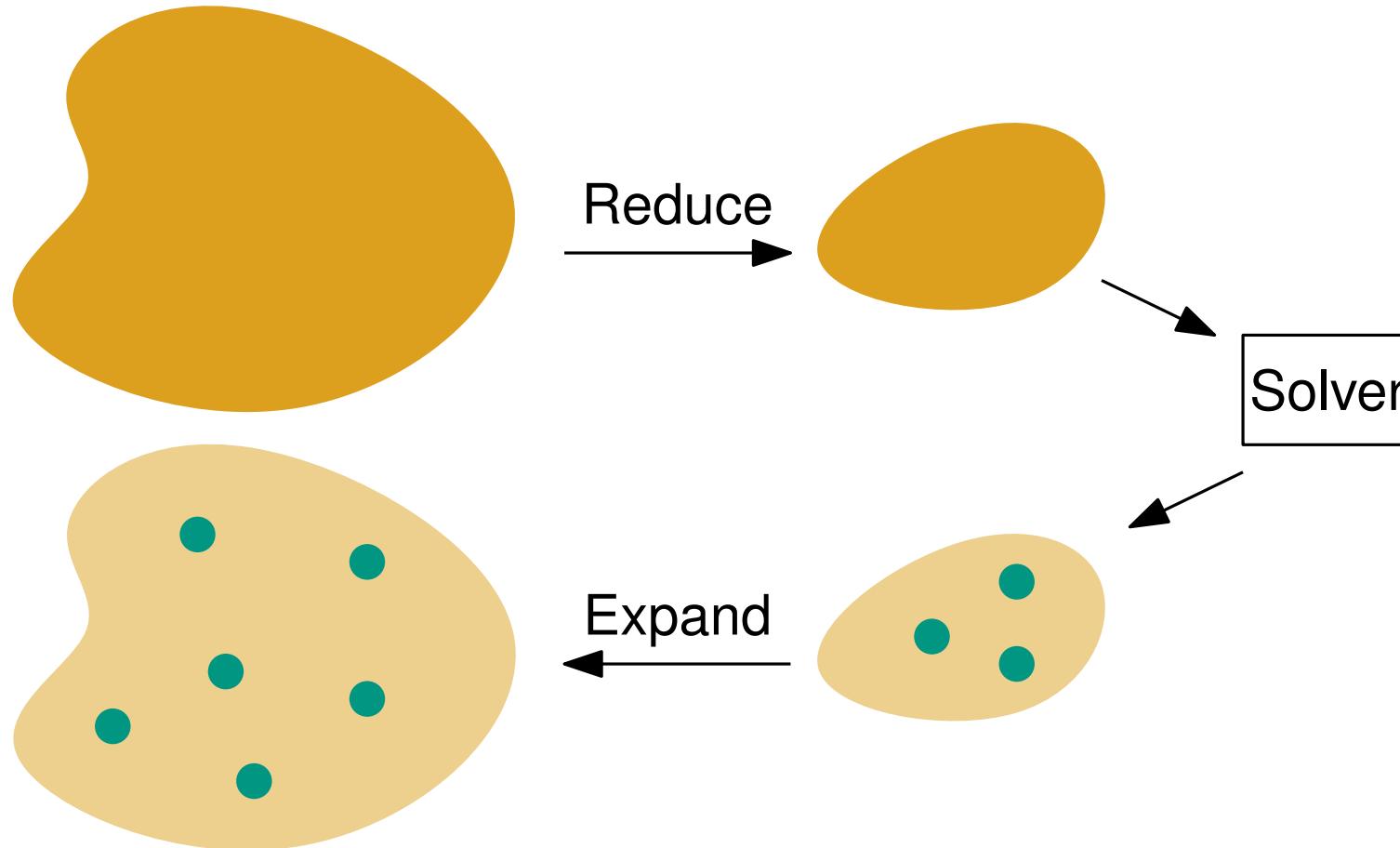
Branch-and-Reduce



Iterated Local Search

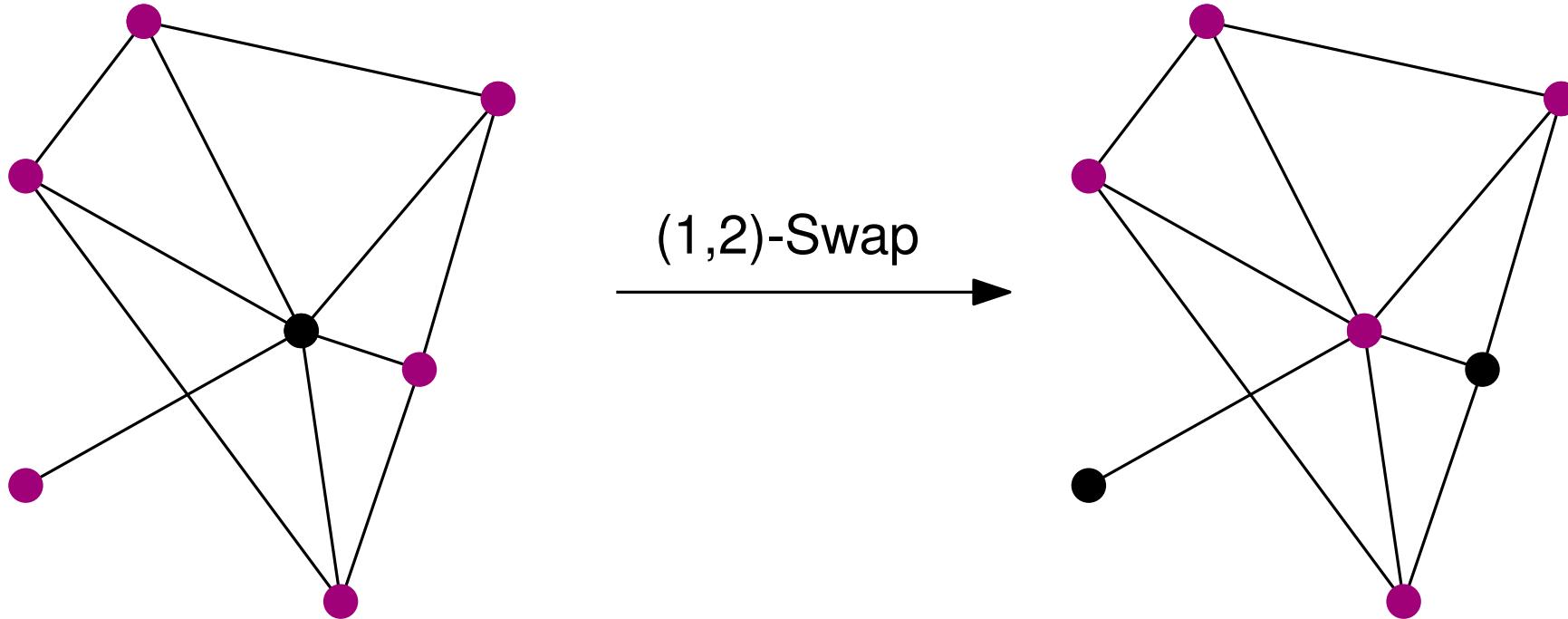


Kernelization [AI2016]



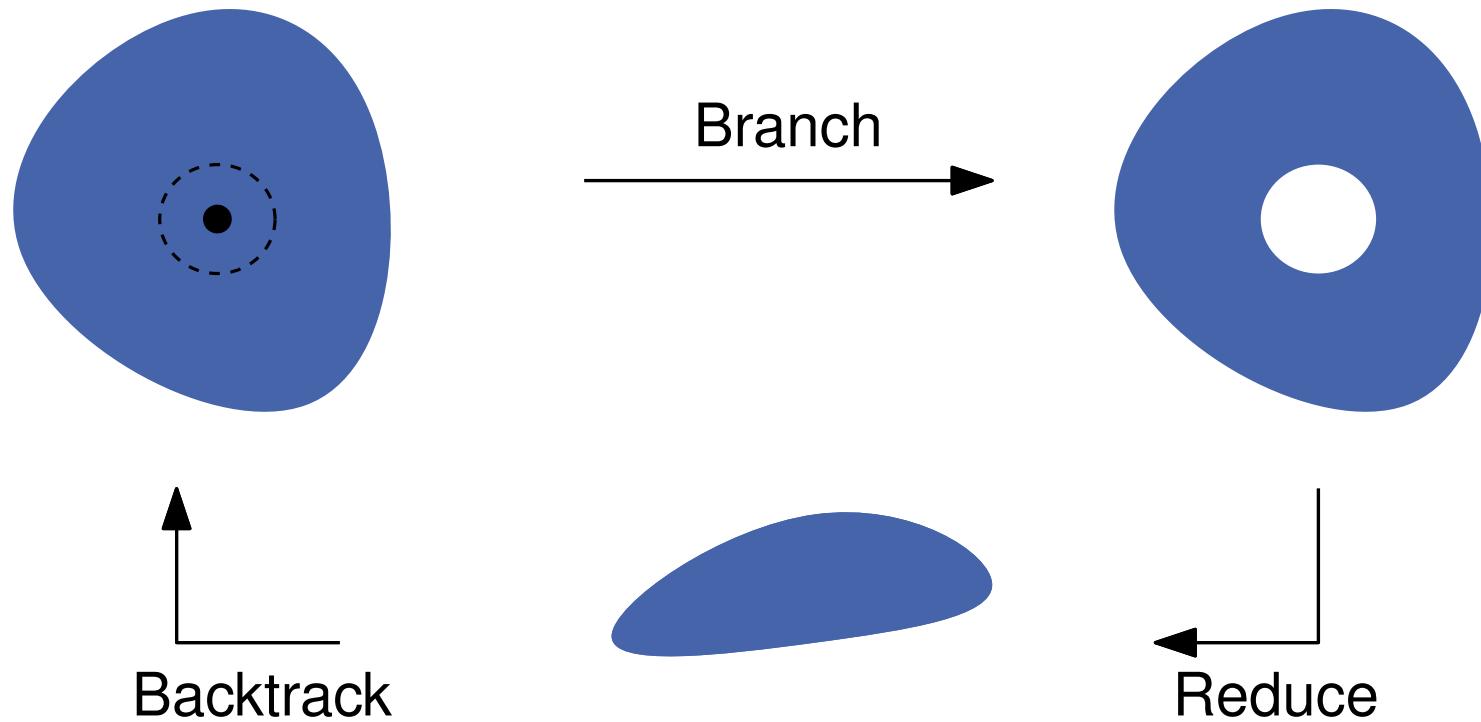
- Technique from FPT algorithms
- Applies rich set of reduction rules
- Significantly reduces graph size

Iterated Local Search [ARW2012]



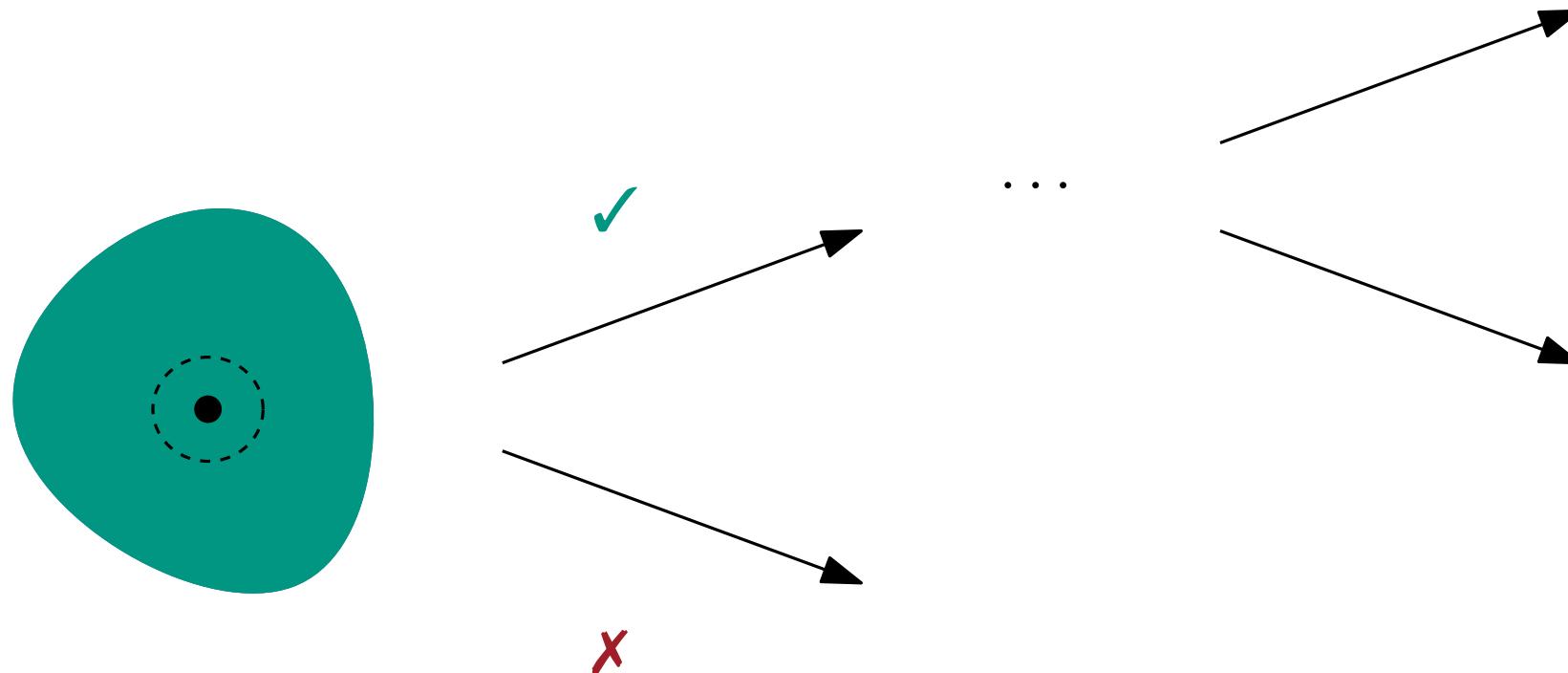
- Originally developed for independent sets
- Perturbation to escape local optima
- Can often find (near-)optimal solutions

Branch and Reduce [AI2016]



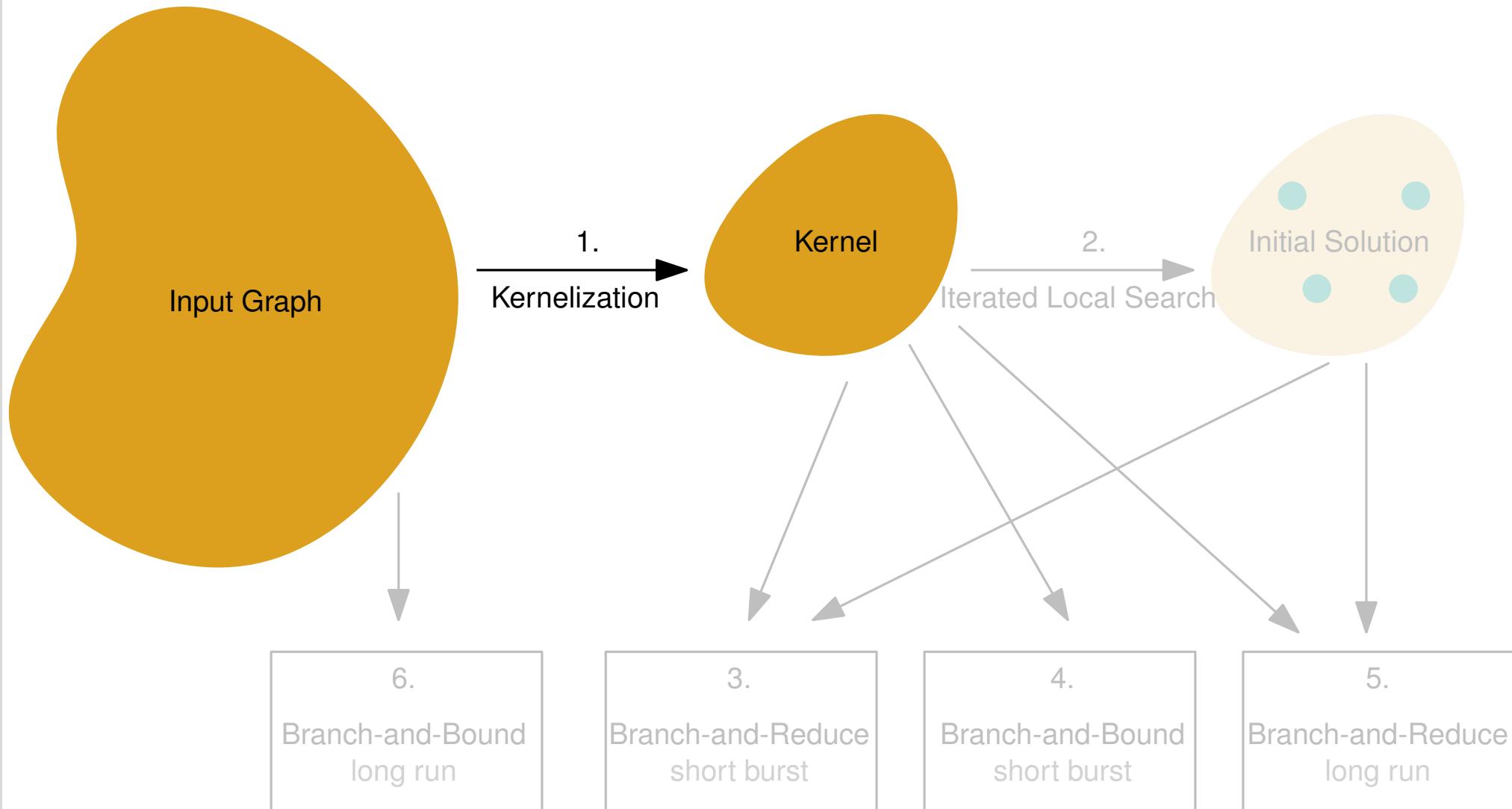
- Reduce graph after each branch
- Additional branching rules to reduce graph size
- Prune search based on lower bounds

Branch and Bound [LJM2017]

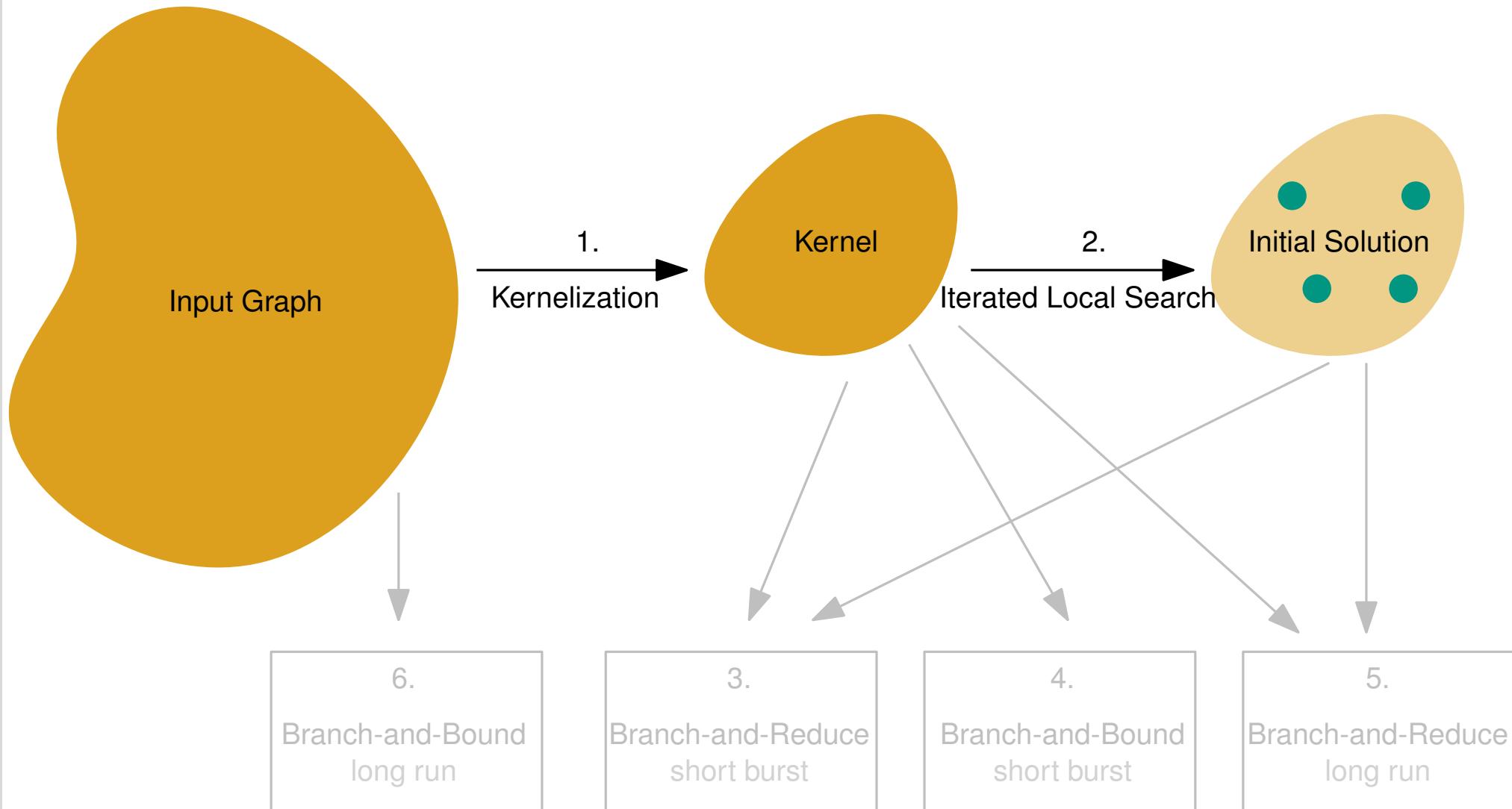


- Originally developed for maximum cliques
- Incremental MaxSAT reasoning to prune search
- Combination of static and dynamic vertex ordering

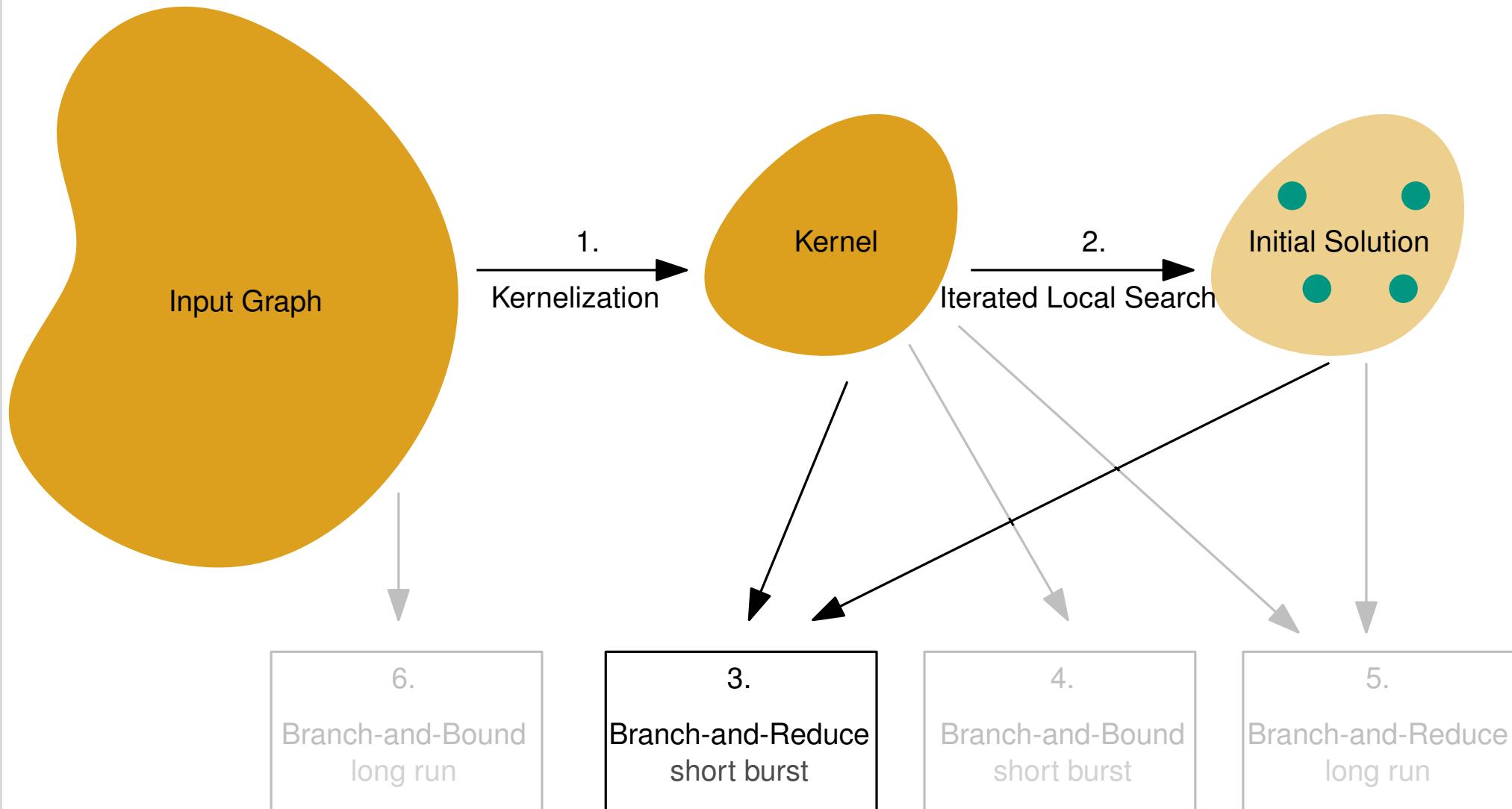
Algorithm Overview



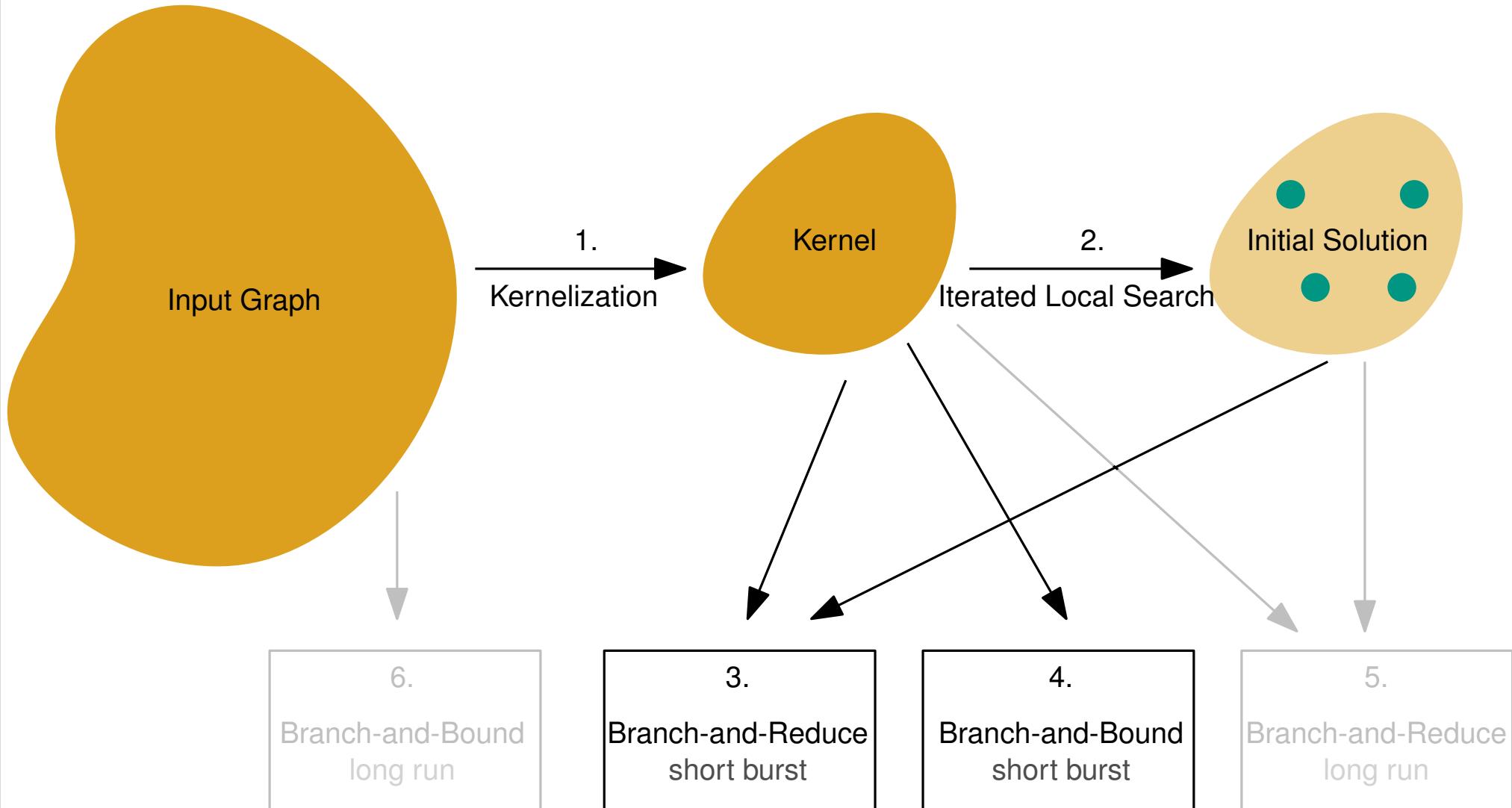
Algorithm Overview



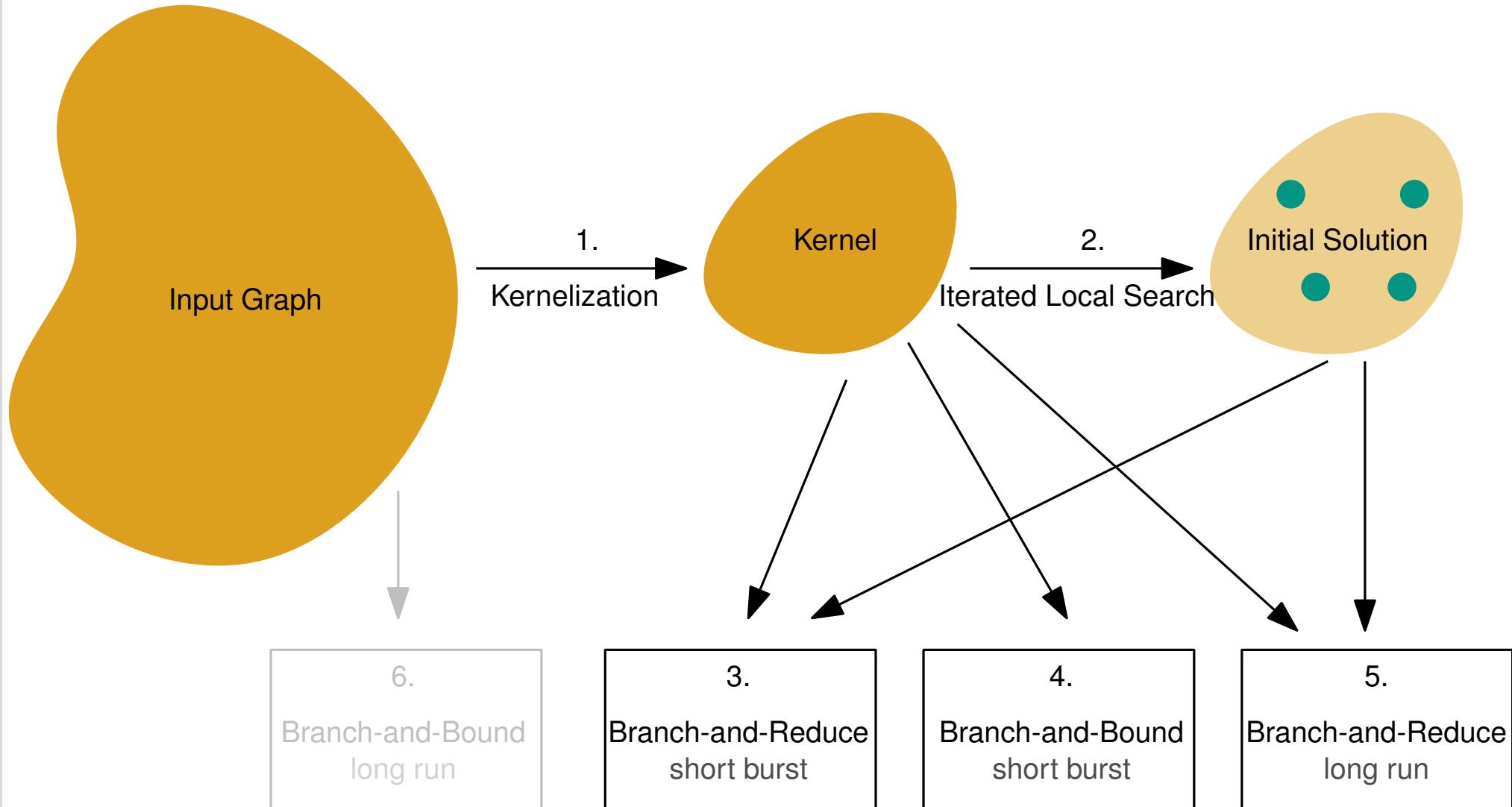
Algorithm Overview



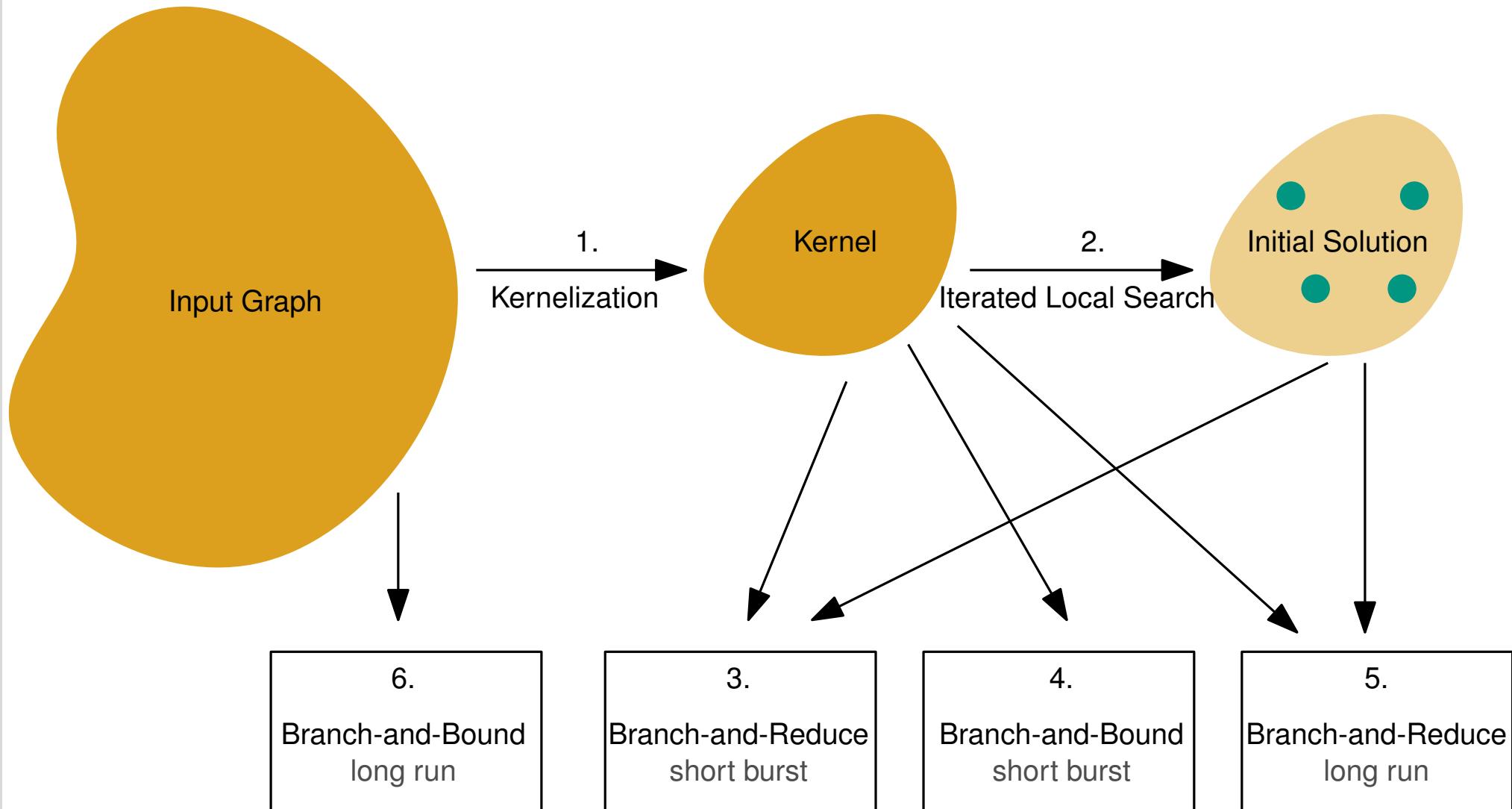
Algorithm Overview



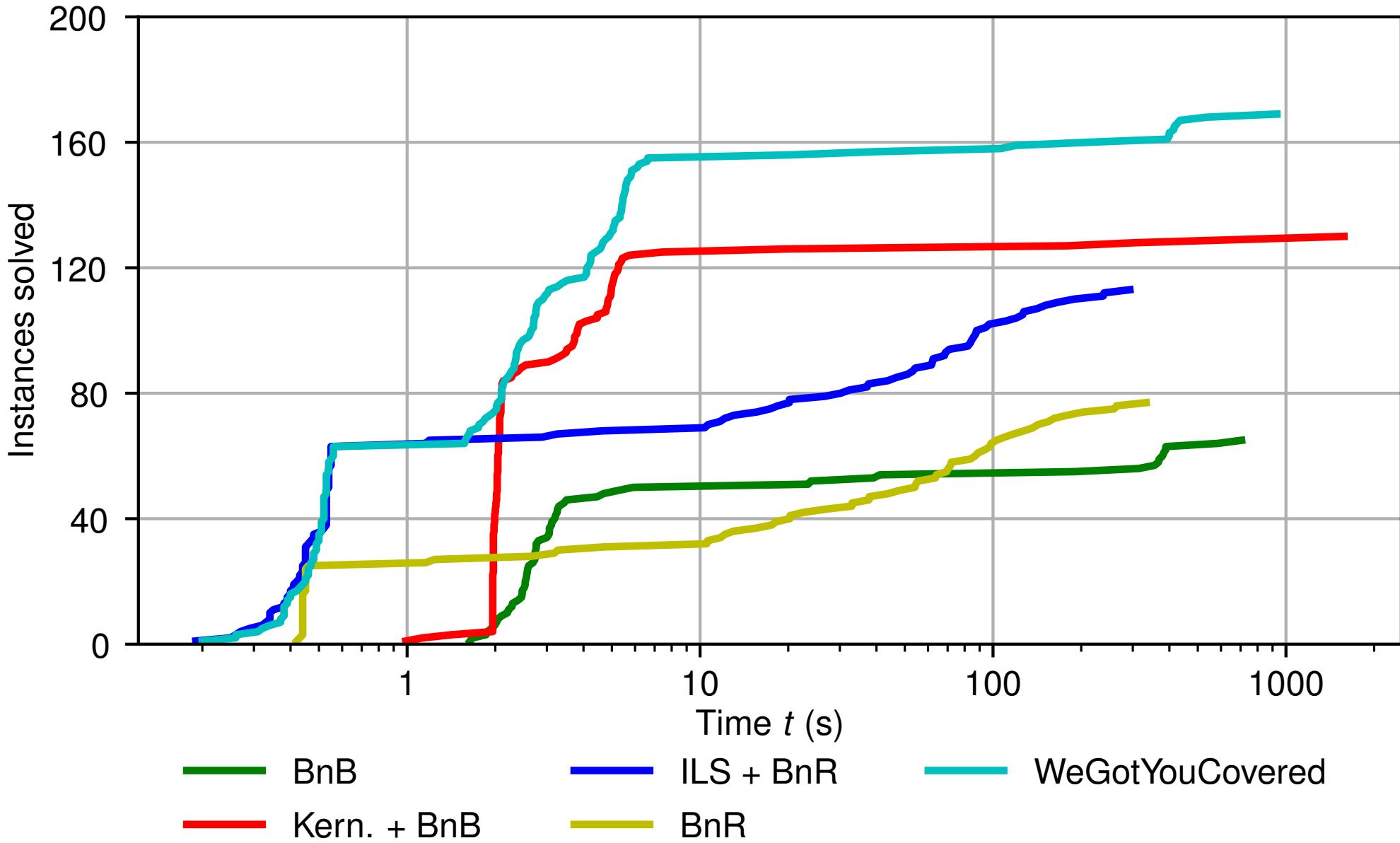
Algorithm Overview



Algorithm Overview



Instances Solved Over Time



References

- Akiba, Takuya, and Yoichi Iwata. “Branch-and-reduce exponential/FPT algorithms in practice: A case study of vertex cover.” *Theoretical Computer Science* 609 (2016): 211-225.
- Andrade, Diogo V., Mauricio G. C. Resende, and Renato F. Werneck. “Fast local search for the maximum independent set problem.” *Journal of Heuristics* 18.4 (2012): 525-547.
- Hespe, Demian, Sebastian Lamm, Christian Schulz and Darren Strash “WeGotYouCovered: The Winning Solver from the PACE 2019 Implementation Challenge, Vertex Cover Track.” *arXiv preprint arXiv:1908.06795* (2019).
- Li, Chu-Min, Hua Jiang, and Felip Manyà. “On minimization of the number of branches in branch-and-bound algorithms for the maximum clique problem.” *Computers & Operations Research* 84 (2017): 1-15.