

Efficient Route Compression for Hybrid Route Planning

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Institute of Theoretical Informatics, Algorithmics II



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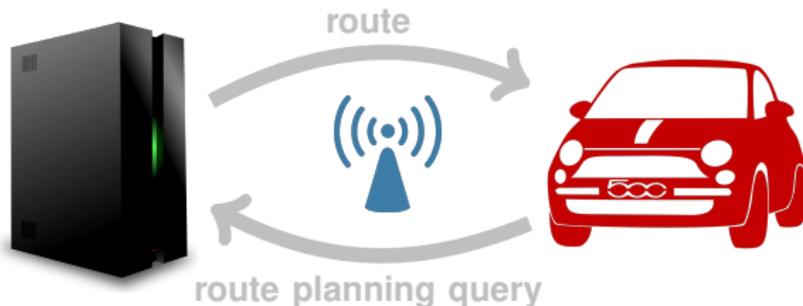
Motivation

Why is **hybrid** route planning **interesting**?

Why is it a **problem**?

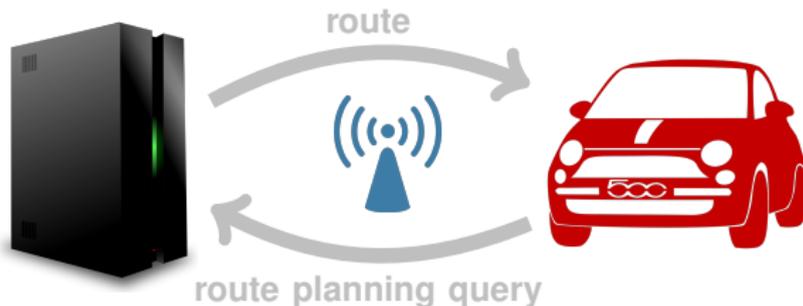
Mobile vs. Hybrid Route Planning

- **Mobile route planning:**
Routes computed by **mobile device** in the car
- **Hybrid route planning:**
Routes computed by **server**, then **transmitted** to car



Mobile vs. Hybrid Route Planning

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⇒ Hybrid route planning requires **mobile radio** communication

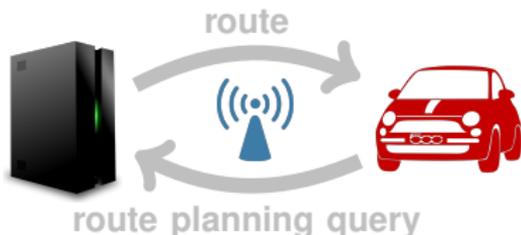
Benefits of Hybrid Route Planning

Advanced route planning algorithms

- high quality routes within milliseconds
- suited for server systems
- difficult to adapt to mobile devices

Hybrid route planning...

- makes server algorithms...
- ...available to car drivers



Time-dependent route planning:

[TD SHARC 08] [TCH 09] [ATCH 10] [Brunel et al. 10] [Batz, Sanders 12]

- exploit **statistical** data, e.g., rush hour
- yields **time-dependent** edge **weights**
- route depends on **time of day**



Flexible route planning:

[flexible CH 10]

- dynamically **fine tune** cost function...
- ...with a **parameter**: $c_e + p \cdot d_e$
- **tradeoff**, e.g., energy cost **vs.** travel time

Server-Based Route Planning (1)

Time-dependent route planning:

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Customizable route planning:

[Delling et al. 11]

- dynamically **change** cost function
- e.g., **unexpected** traffic situations

Multi-criteria route planning:

[Delling, Wagner 09]

- deal with **multiple incomparable** costs
- e.g., **travel time** vs. **inconveniency**



Server-Based Route Planning (2)

Customizable route planning:

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Alternative routes:

[Abraham et al. 10] [Luxen, Schieferdecker 12]

- a **handful** of alternatives
- **nearly** as good as optimal route
- reasonable **different**



Hub-labeling algorithms:

[Abraham et al. 11] [Abraham et al. 12]

- running times $< 1 \mu\text{s}$ implemented with **C++**
- fast route planning with **database** servers
- more **complicated** queries, e.g., route via **POI**

Server-Based Route Planning (3)

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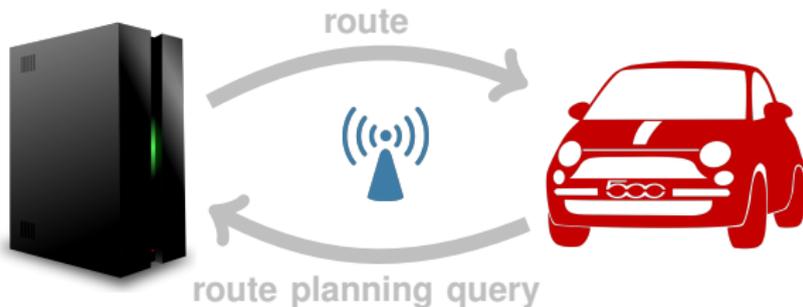
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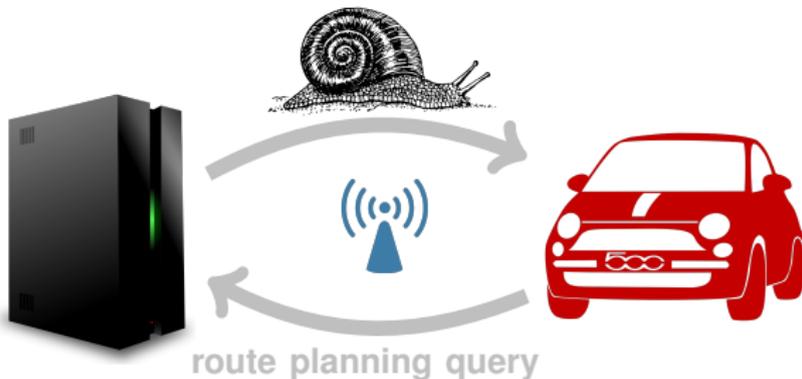
Problems with **Radio** Communication

- Low **bandwidth**, but **complex** routes
- Transmission **costs**



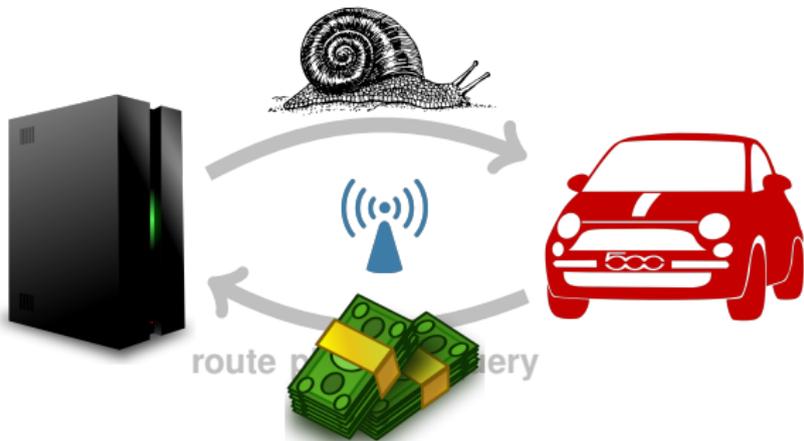
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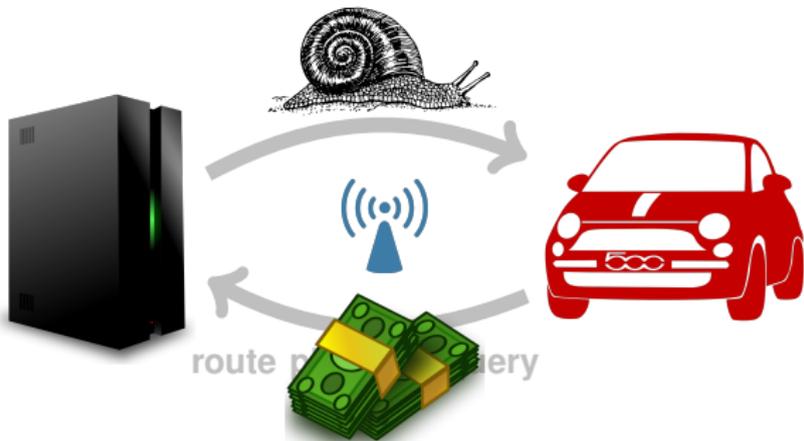
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⇒ **Do data **compression!****

Contribution

Efficient lossless **compression** of routes.

Compression of Routes

To Make **Hybrid** Route Planning **Convenient** to Use

Fast: User **experiences** no delay

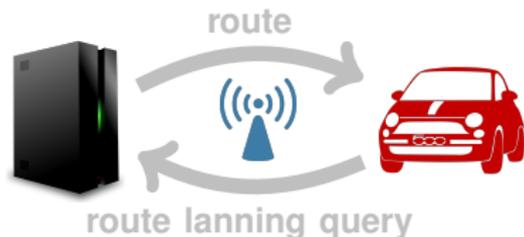
- Driving directions **start** within ≤ 0.1 sec.
- **Fast** compression / decompression / transmission

Lossless:

- **Reconstructed** route = **server-provided** route

Resulting Requirements:

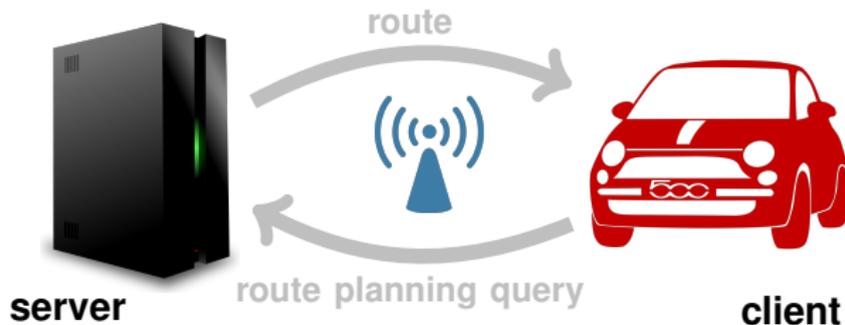
- Fast **algorithms**
- Good compression **rates**



Basic Setup...

...Needed by our Approach

- Client has **basic** and **fast** route planning capability
- Client and Server use **same** road network
- Client uses **fixed** cost function **known** to the **server**



Basic Idea: Use Via Nodes

server



client

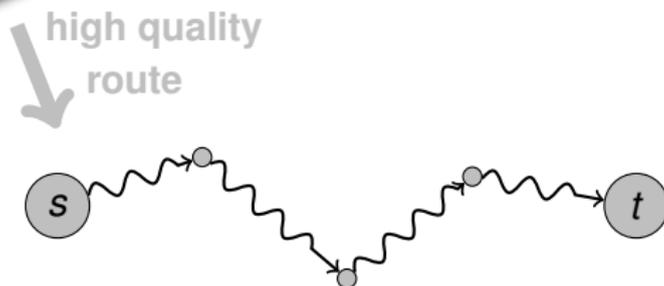


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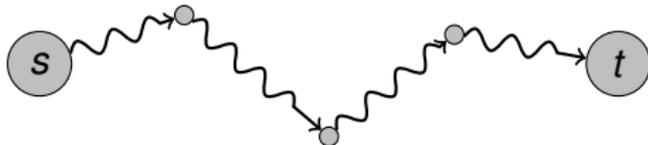


client

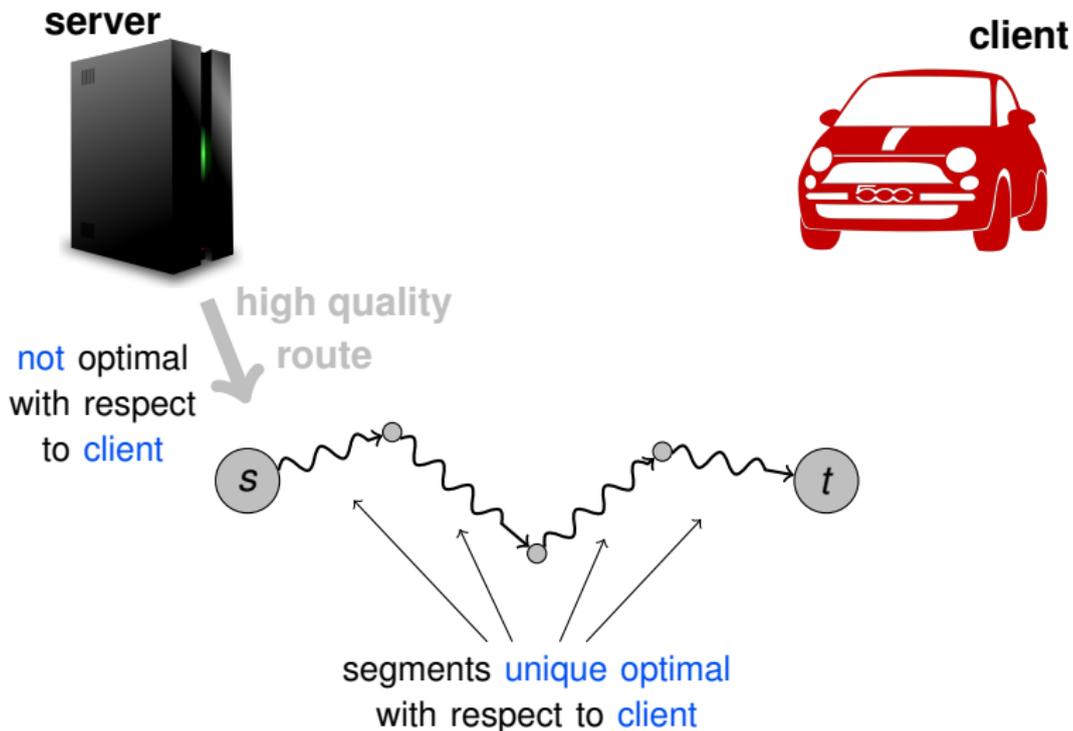


not optimal
with respect
to client

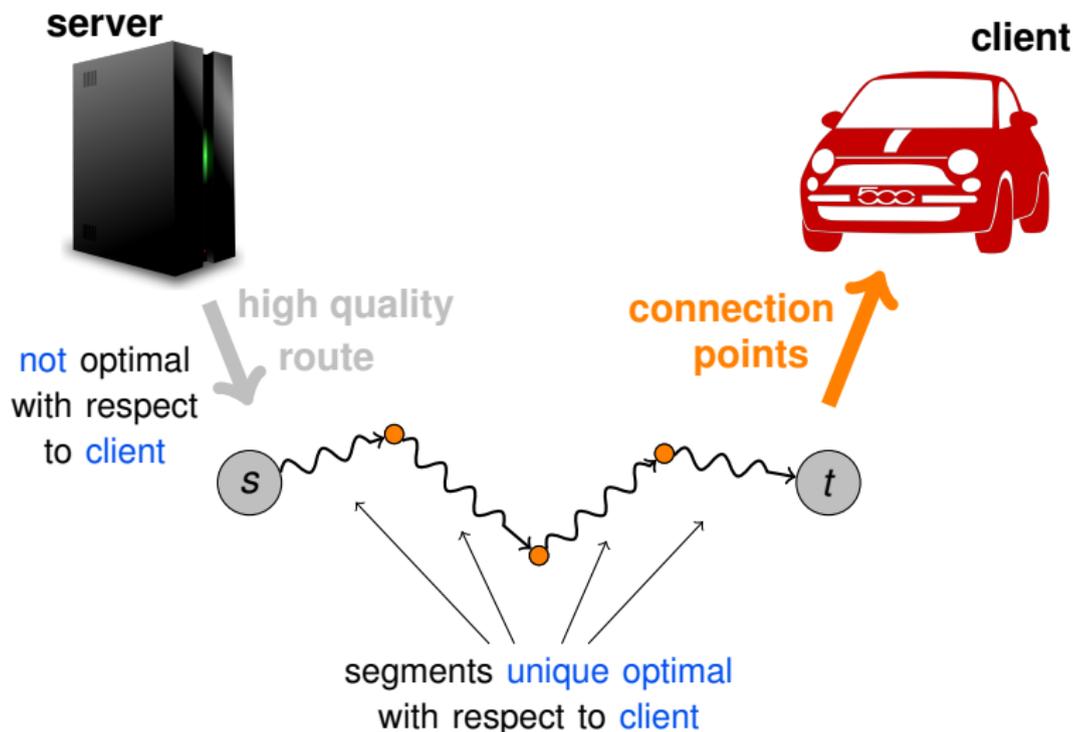
high quality
route



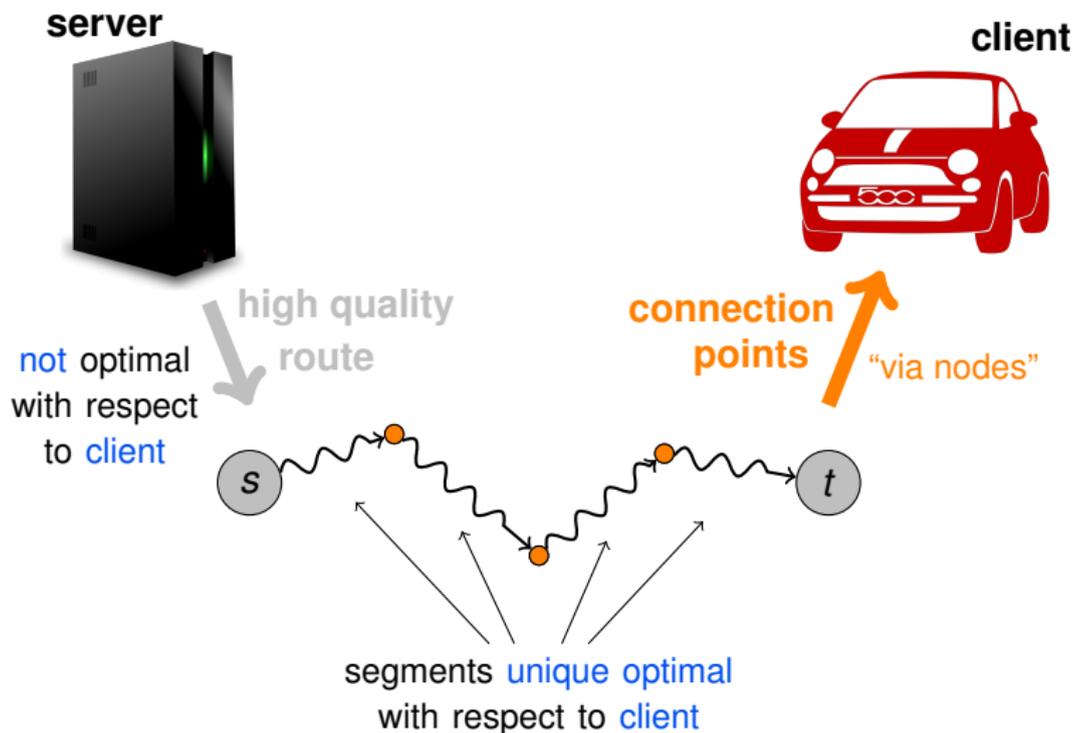
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Compression with Via Nodes

Exact Definition

Road network

- Directed graph $G = (V, E)$
- Edge weights **client**: $c(u, v) \in \mathbb{R}_{\geq 0}$ (simple!)
- Edge weights **server**: **not** needed

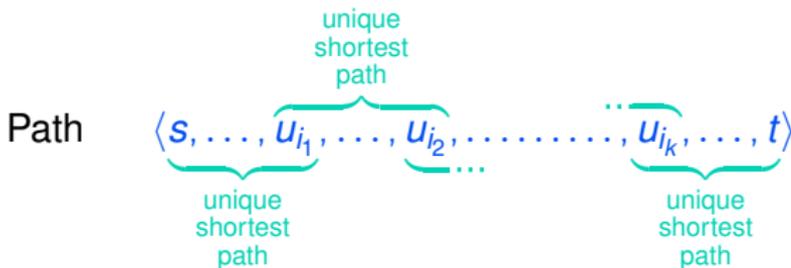
Path $\langle s, \dots, u_{i_1}, \dots, u_{i_2}, \dots, u_{i_k}, \dots, t \rangle$

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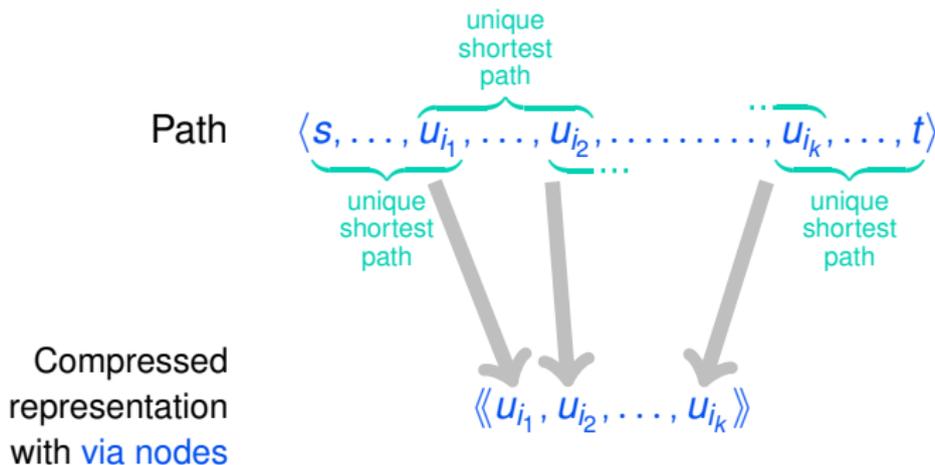


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Compression with Via Nodes

Method for Decompression

- Compute shortest paths between via nodes
- Mobile CH do this in 0.1 sec. [ESA 08]
- Uniqueness \Rightarrow correctness



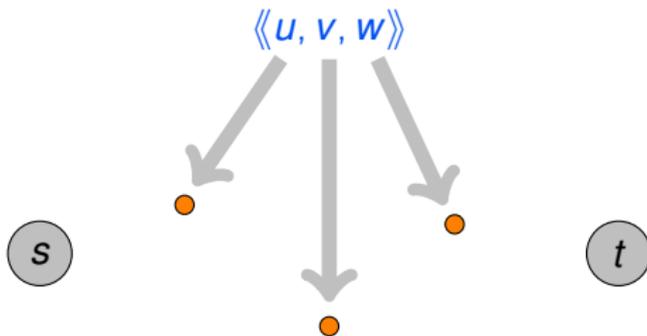
$\langle\langle u, v, w \rangle\rangle$



Compression with Via Nodes

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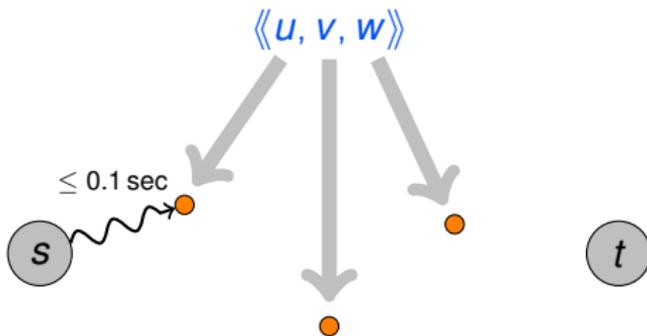
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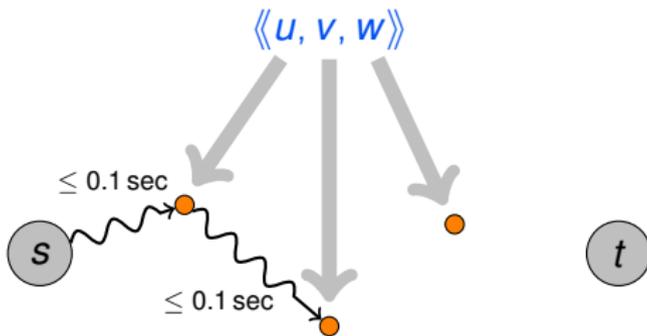
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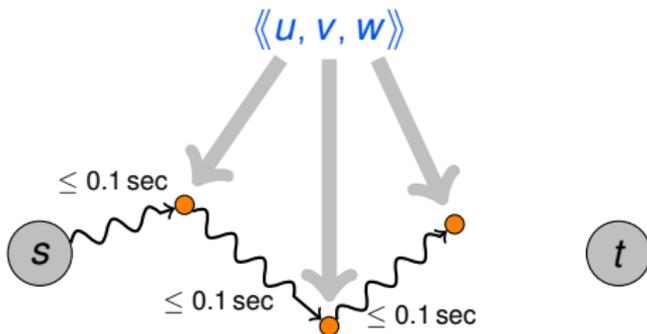
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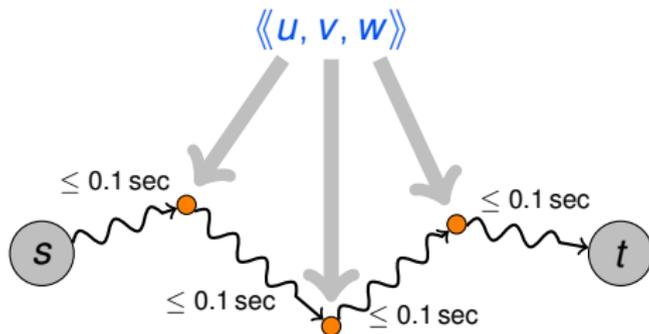
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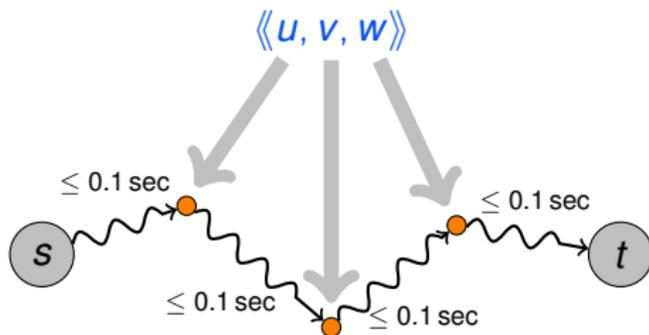
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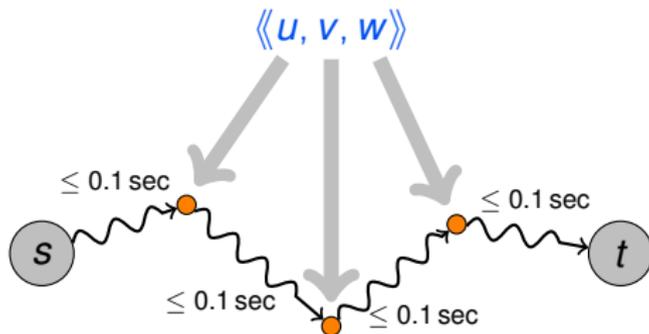


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\Rightarrow **Driver experiences no delay!**

\Rightarrow **Convenient to use.**

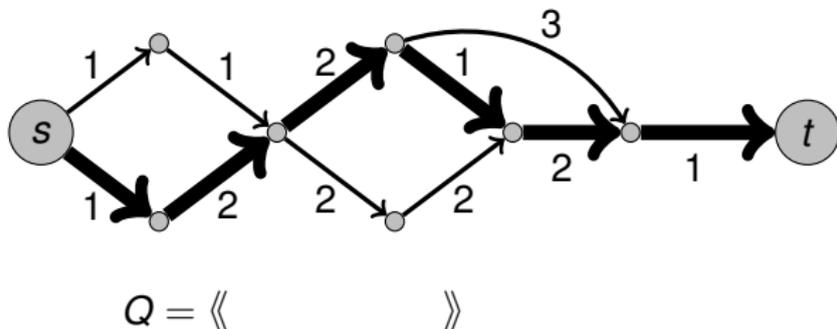
Compression with Via Nodes

Frame Algorithm for Compression



Compress path P

- $Q := \langle \rangle$
- Repeatedly
- remove the maximal unique shortest prefix from P
- each appending its last node to Q



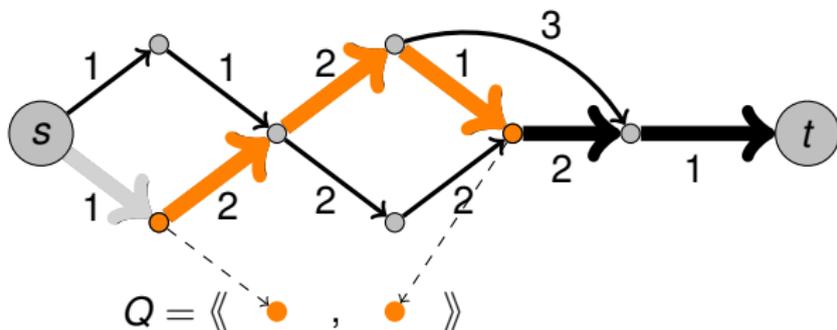
⇒ Finds minimal number of via nodes

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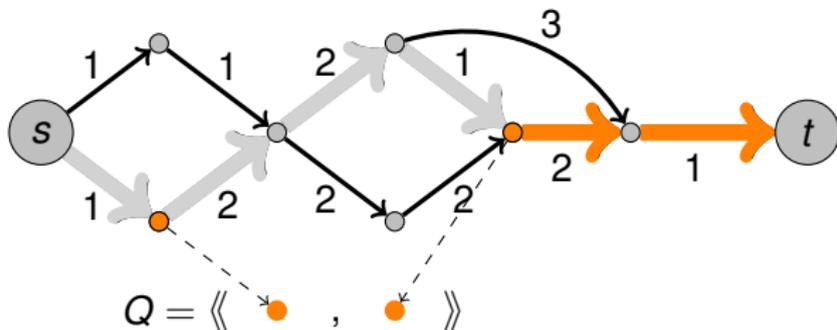
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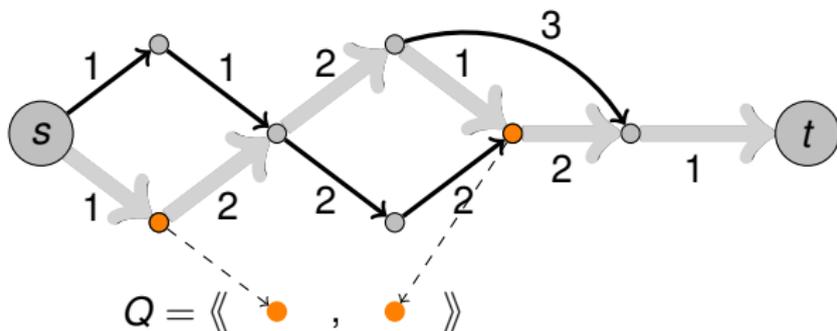
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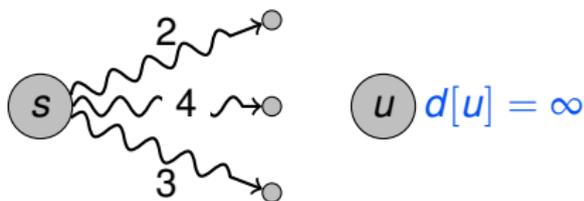


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Find **Maximal Unique Shortest Prefix**

Modified Dijkstra – simple but **slow**

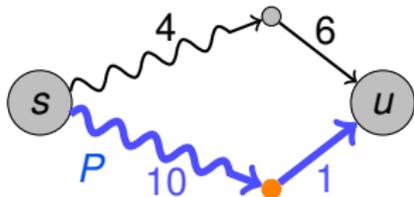


Relaxing an edge:

- Mark node when **non-uniquely** reached
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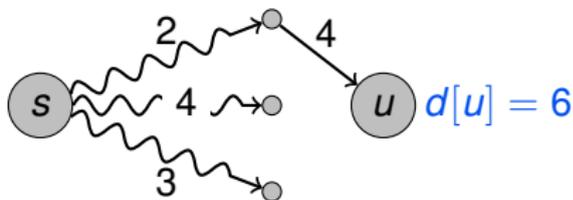
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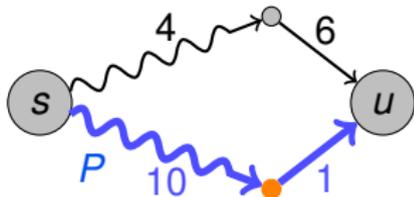


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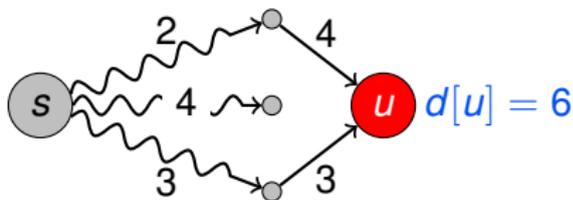
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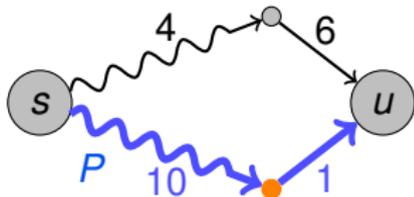


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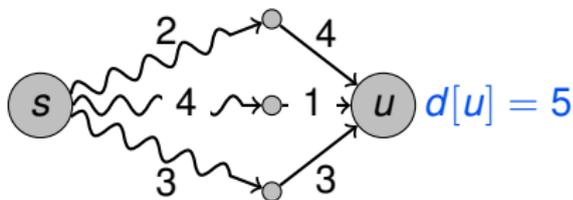
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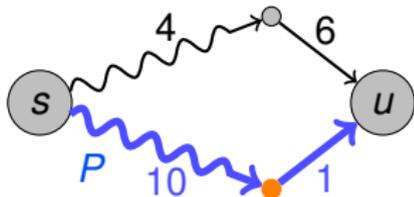


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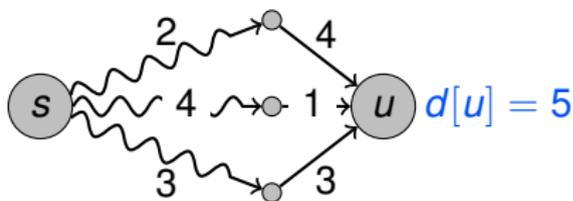
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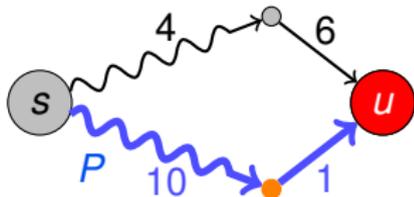


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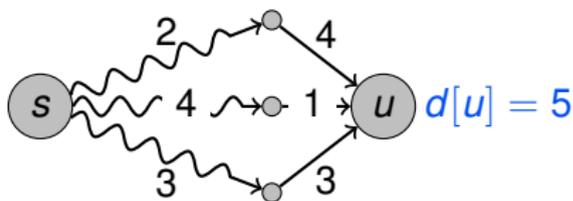
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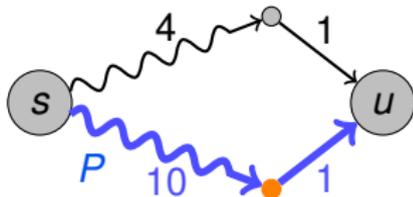


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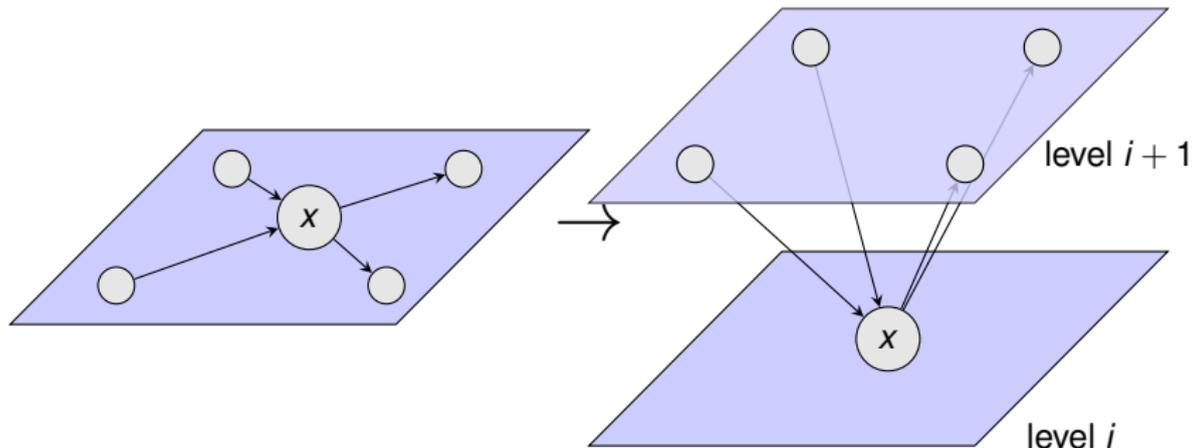


Contraction Hierarchies (CH)

[Geisberger et al. 08]

Construct a hierarchy in a **preprocessing** step:

- Order nodes by importance
- Obtain next level by **contracting** next node
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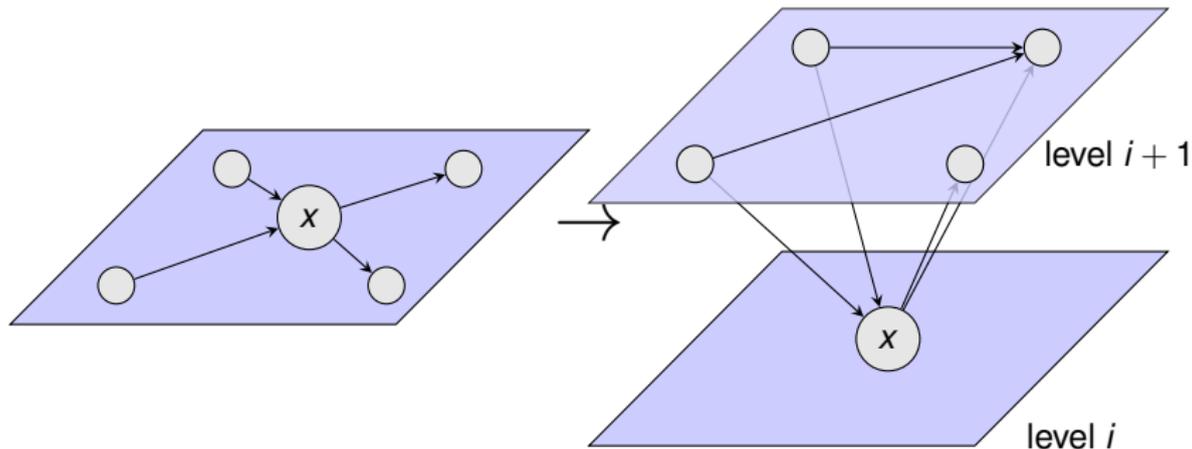


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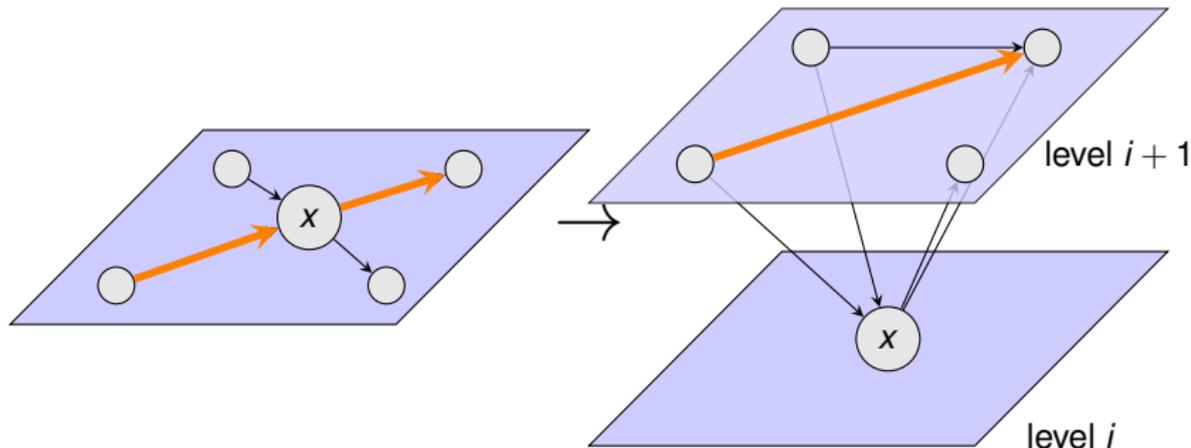


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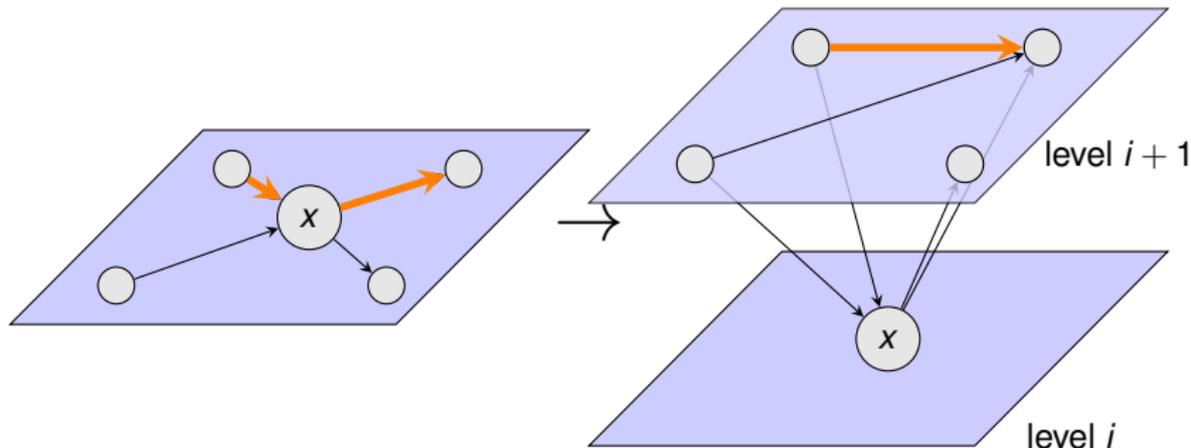


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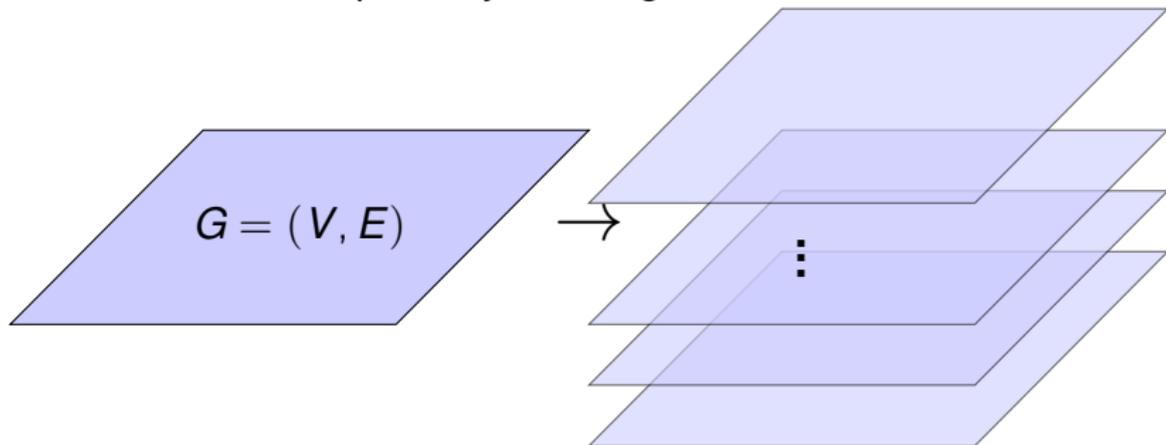


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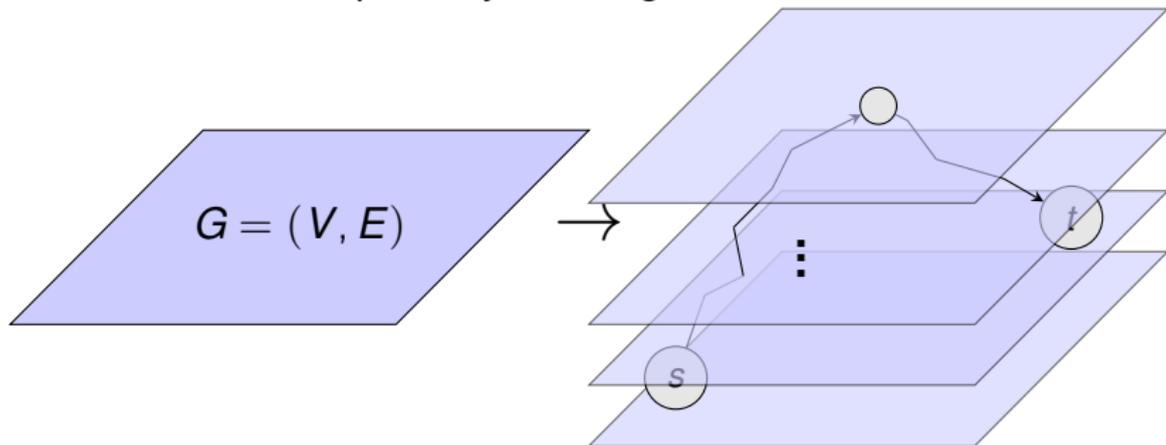


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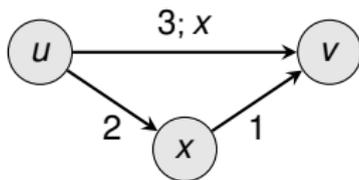
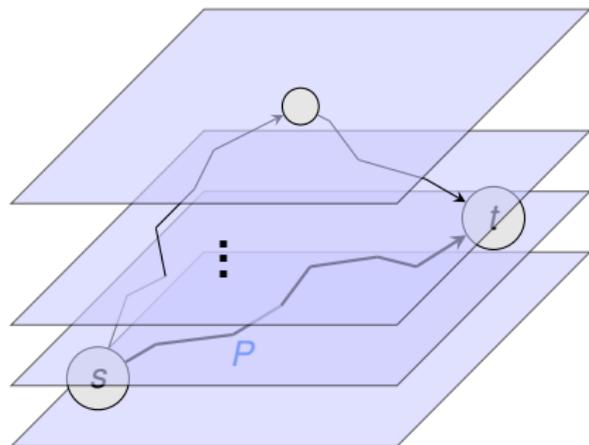
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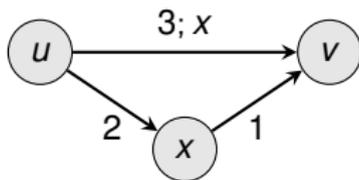
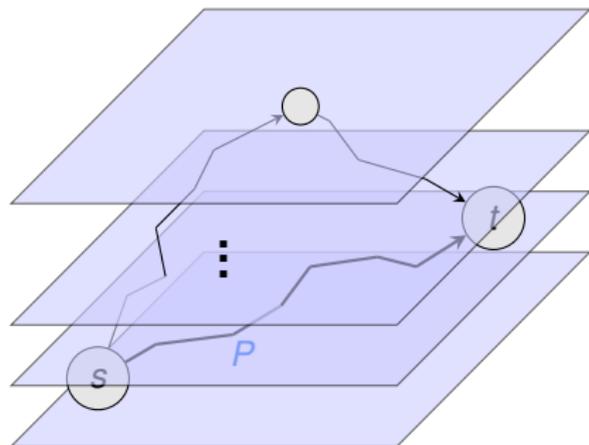
⇒ There is always a shortest **up-down-path** from **s** to **t**.

Representing Paths with CH Uniquely



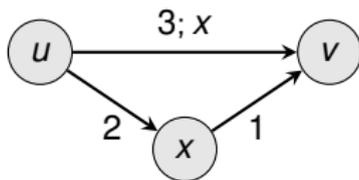
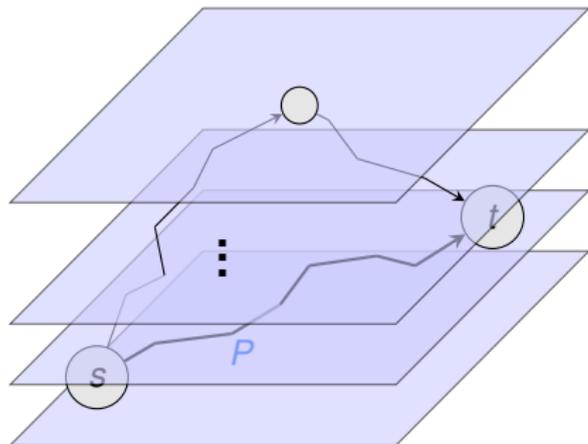
- Shortcuts can be expanded recursively
- Up-down-paths contain several shortcuts
- Expand these shortcuts completely
⇒ An up-down-path represents an original path

Representing Paths with CH Uniquely

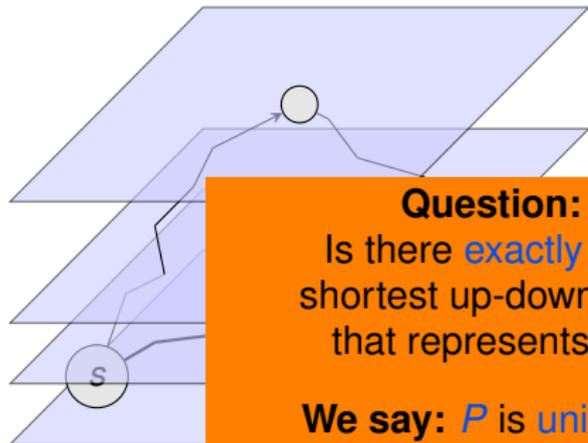


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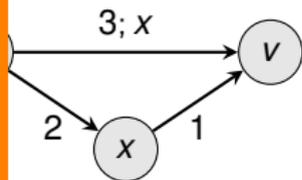
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Question:

Is there **exactly one** shortest up-down path that represents P ?

We say: P is **uniquely CH-representable**

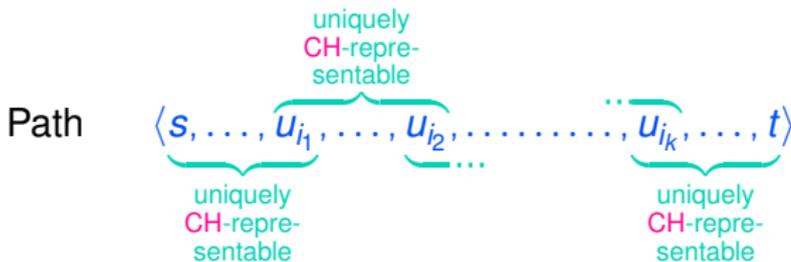


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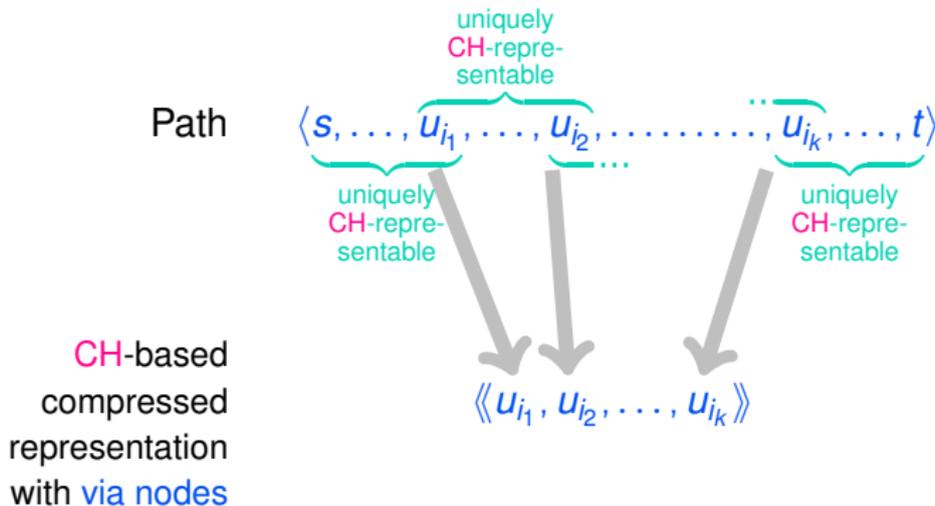
CH-Based Representation of a path with **Via Nodes**

Path $\langle s, \dots, u_{i_1}, \dots, u_{i_2}, \dots, u_{i_k}, \dots, t \rangle$

CH-Based Representation of a path with Via Nodes



CH-Based Representation of a path with Via Nodes



Compression with Via Nodes

Frame Algorithm for Compression

Compress path P

- $Q := \langle \rangle$
- **Repeatedly**
- remove the maximal uniquely CH-representable prefix from P
- each appending its last node to Q



Find Uniquely CH-Representable Prefix

Inspired by Binary Search

Find uniquely CH-representable prefix of path $\langle u_1, \dots, u_n \rangle$

- $(\ell, m, r) := (1, n, n)$
- **while** $\ell + 1 < r$ **do**
- **if** $\langle u_1, \dots, u_m \rangle$ is uniquely CH-representable **then** $\ell := m$
- **else** $r := m$
- $m := \lfloor \ell + 1 + r \rfloor$
- **od**
- **return** $\langle u_1, \dots, u_\ell \rangle$

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⇒ Checks $O(\log n)$ times whether uniquely CH-representable.

How to Find a Uniquely CH-Representable Prefix

Inspired by Binary Search



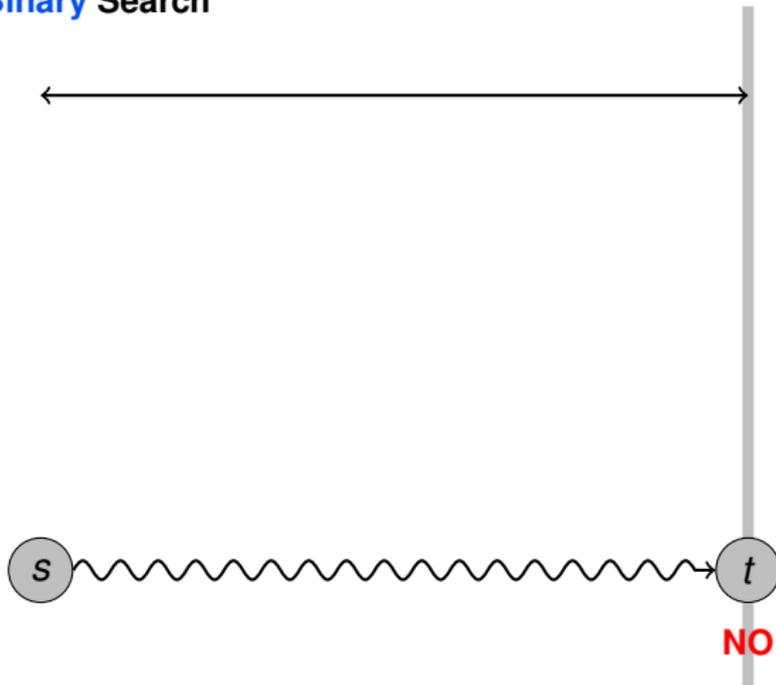
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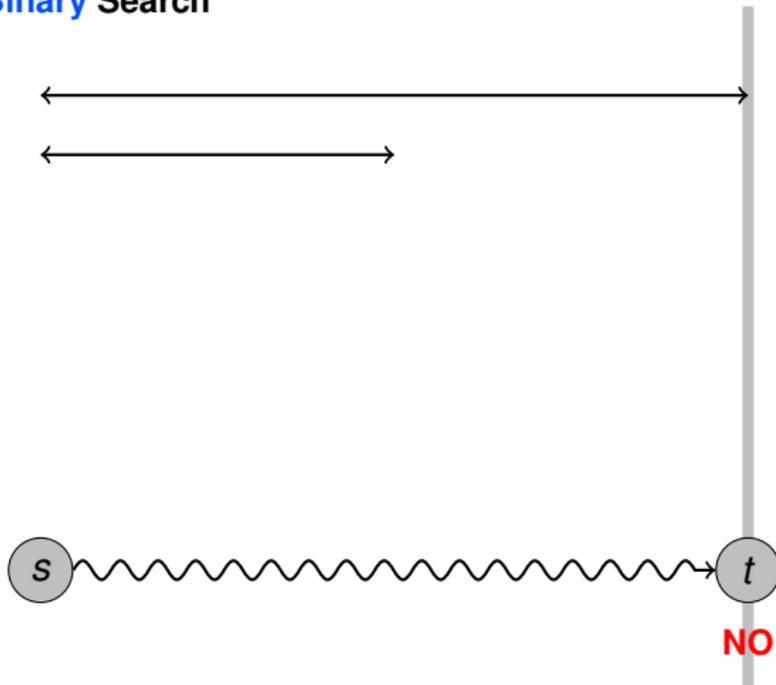
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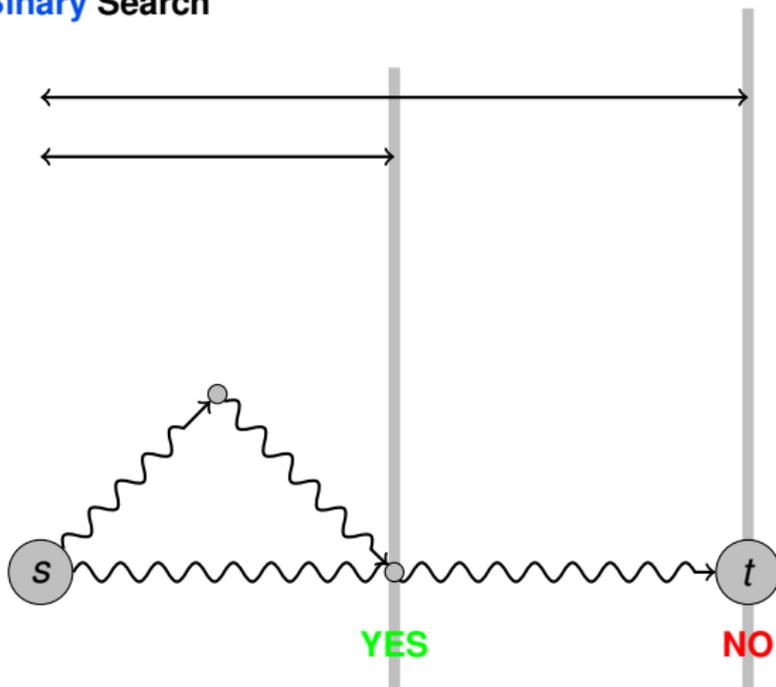
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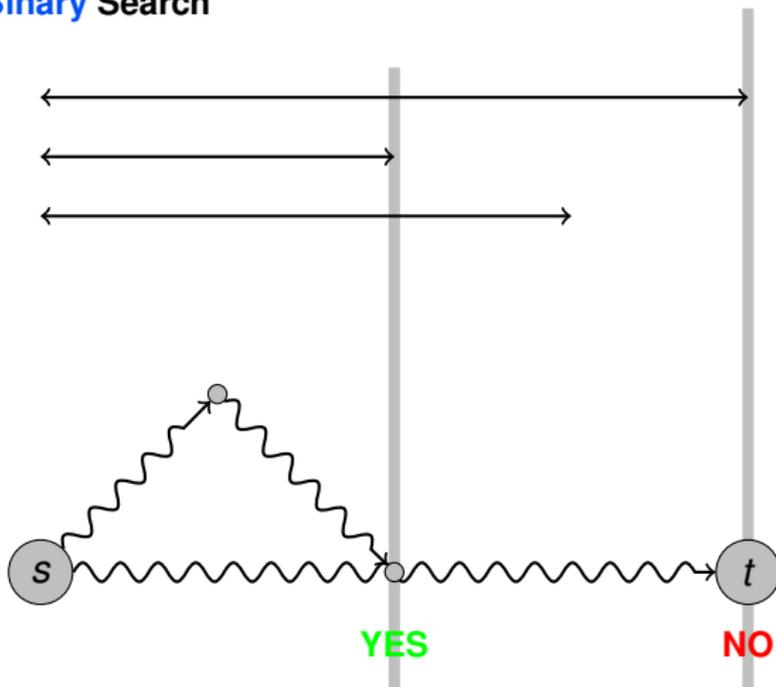
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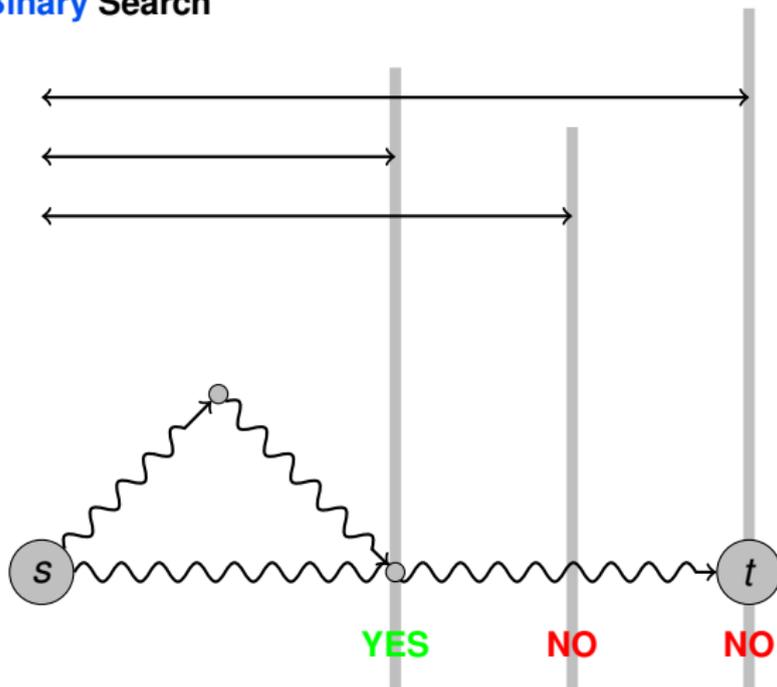
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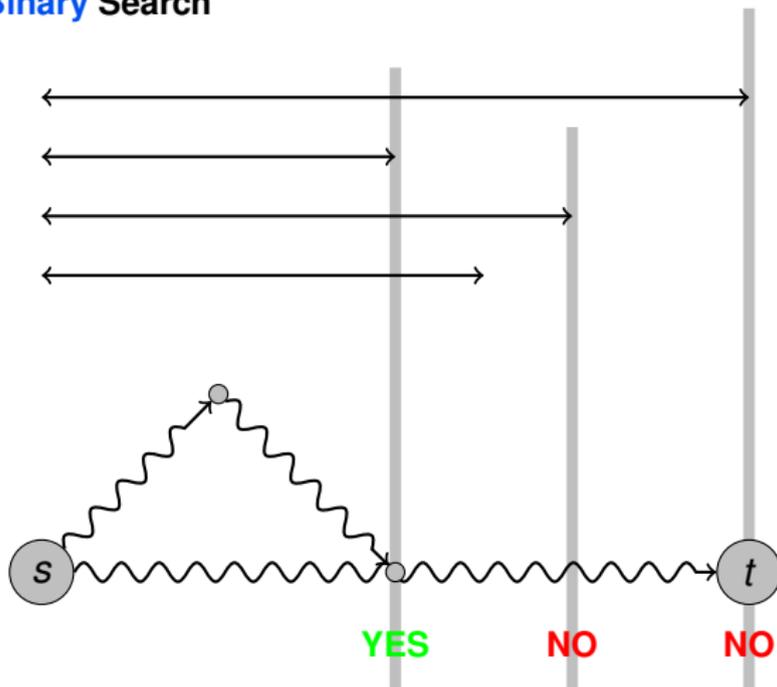
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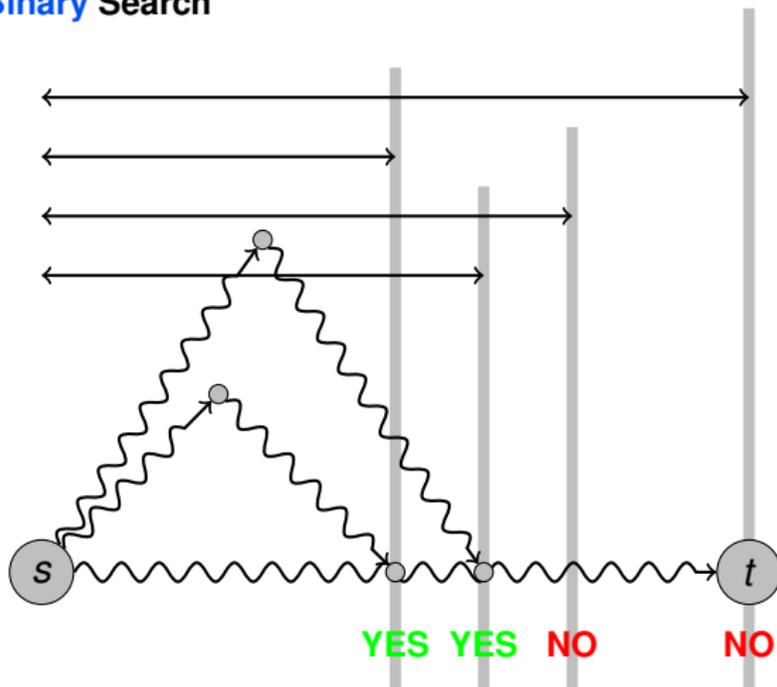
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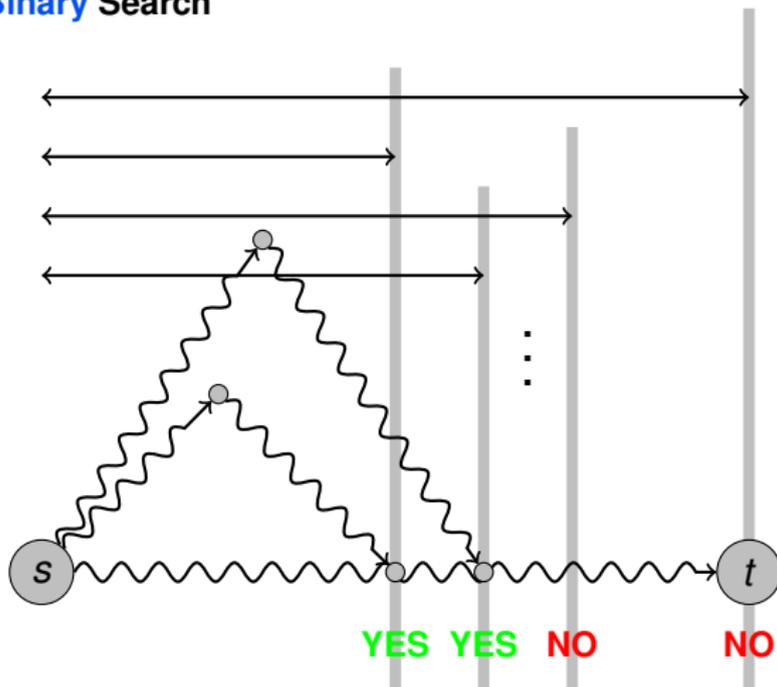
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Inspired by Binary Search



Find Uniquely CH-Representable Prefix

Inspired by **Binary Search**

Find uniquely CH-representable prefix of path $\langle u_1, \dots, u_n \rangle$

■ $(\ell, m, r) := (1, n, n)$ **Theorem:**

Found prefix contains **unique shortest prefix** or **more**.

■ **while** $\ell + 1 < r$ **do**

■ **if** $\langle u_1, \dots, u_m \rangle$ **is uniquely CH-representable** **then** $\ell := m$

■ **else** $r := m$

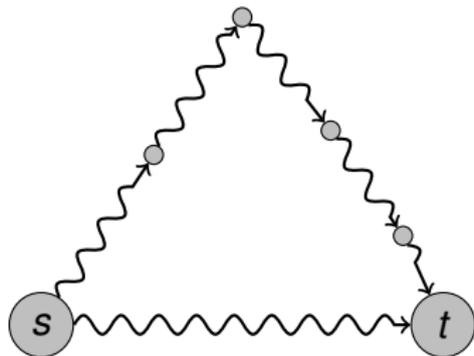
■ $m := \lfloor \ell + 1 + r \rfloor$

■ **od**

■ **return** $\langle u_1, \dots, u_\ell \rangle$

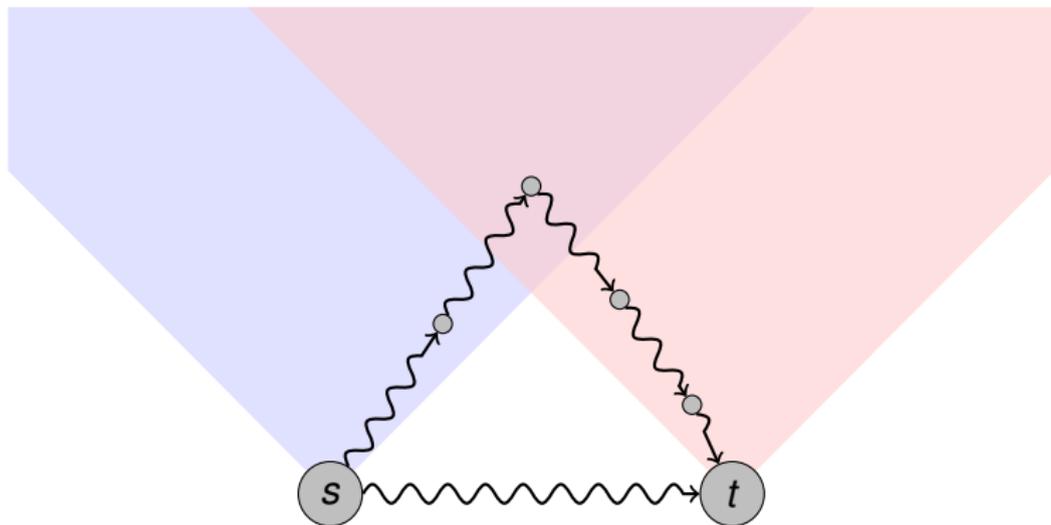
⇒ Checks $O(\log n)$ times whether **uniquely CH-representable**.

How to Check Whether Path is Uniquely CH-Representable



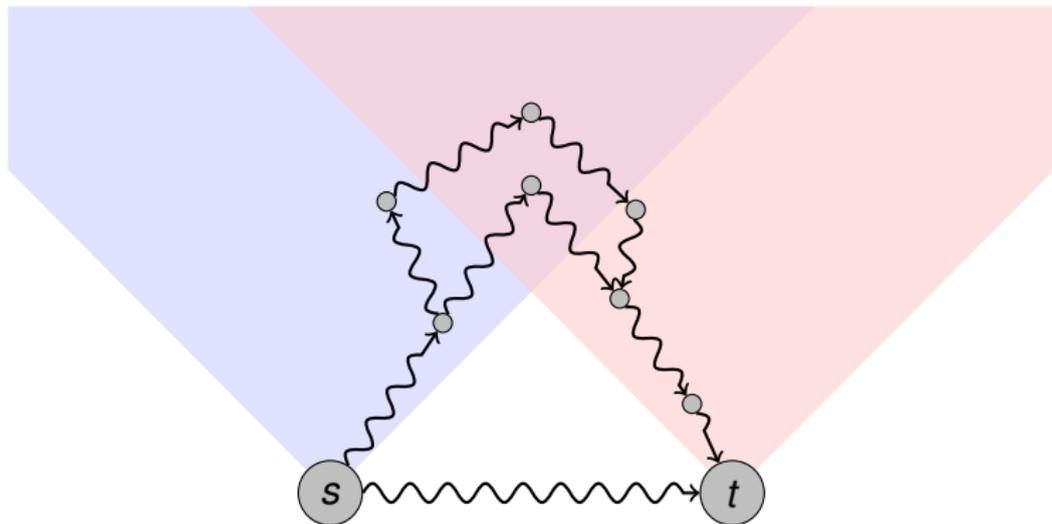
Perform modified **bidirectional** upward **Disjktra** search

How to Check Whether Path is Uniquely CH-Representable



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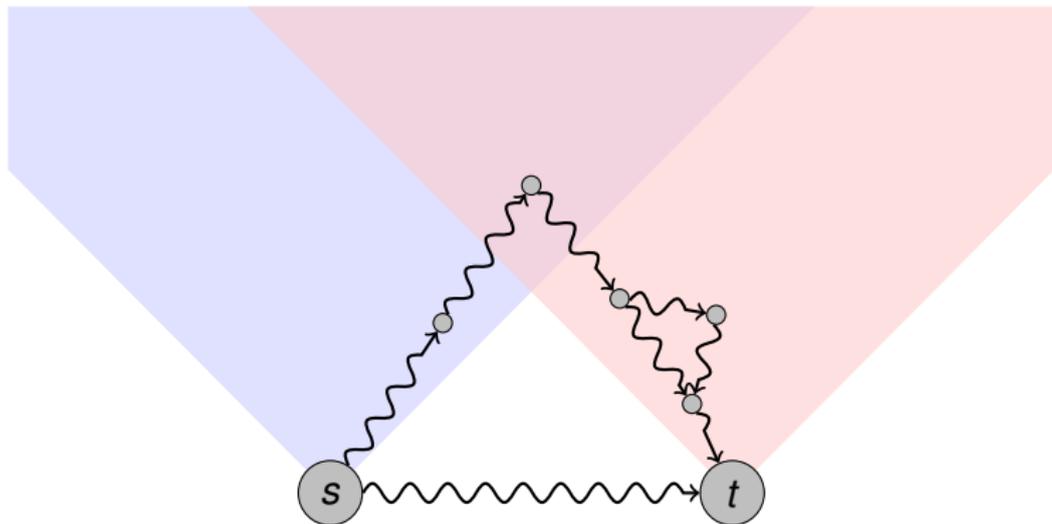
How to Check Whether Path is Uniquely CH-Representable



Perform modified **bidirectional** upward **Disjktra** search

Detect **multiple** top nodes

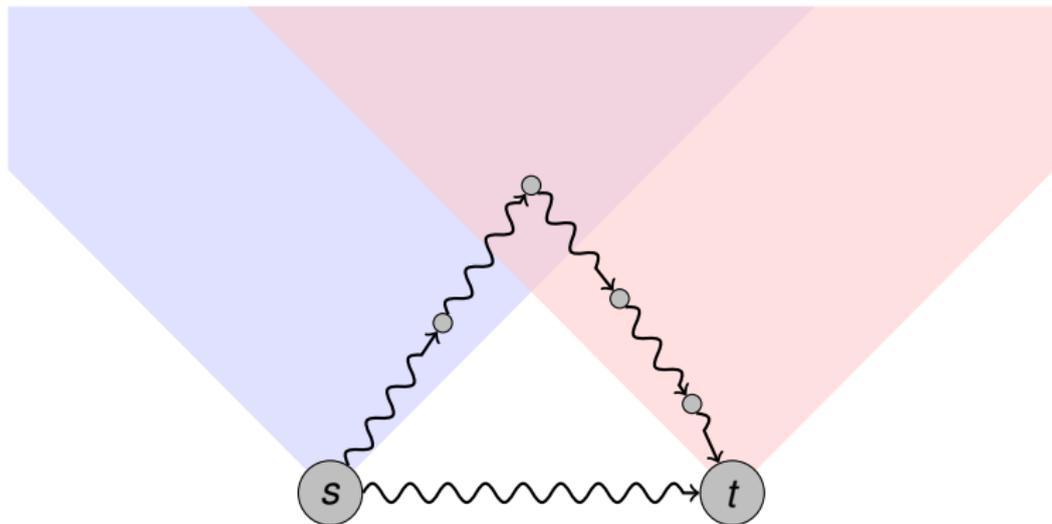
How to Check Whether Path is Uniquely CH-Representable



Perform modified **bidirectional** upward **Disjktra** search

Detect **non-unique** subpaths

How to Check Whether Path is Uniquely CH-Representable



Perform modified **bidirectional** upward **Disjktra** search

This is very fast: Hierarchy is **flat** and **sparse**.

Compression Rate with CH

Lemma:

Unique shortest path \Rightarrow uniquely CH-representable.
 \Leftrightarrow

Consequence:

In theory, CH-based representation can have less via nodes.

Compression with Via Nodes

CH-based Compression – Summary

- **Algorithm:**
Frame-Algor. + binary Scheme + bidir. search in CH
- **Fast:**
 - perform bidir. search $O(\# \text{via nodes} \cdot \log |P|)$ times
 - upward search in flat and sparse hierarchy
- **Compression rate:**
(in theory) even better

Experiments

Compression **Time** and **Rate**.

German road network

- Nodes: 4.7 million
- Edges: 10.8 million, 7.2 % time-dependent

Simulating of Client and Server

- Different metrics...
- ...for route planning and compression

Evaluated compression algorithms

- Frame-Algor. + modified Dijkstra
- Frame-Algor. + binary Scheme + bidir. search in CH
- **Problem:** Our CH-based implementation pessimistic

Four Metrics (1)

Metric = Edge-Weights + Objective

time-dependent

- **Edge-Weights:** Functions f_e : time $\mapsto \Delta$ travel time
- **Objective:** Find earliest arrival route for departure time τ_0

free flow

- **Edge-Weights:** Time-independent travel times $\min f_e$
- **Objective:** Find shortest path

Four Metrics (2)

Metric = Edge-Weights + Objective

distance

- **Edge-Weights:** Driving distance dd_e
- **Objective:** Find **shortest** path

energy

- **Edge-Weights:** Estimate energy cost $dd_e + \gamma \min f_e$
- **Objective:** Find **shortest** path

with $\gamma := 4 \rightsquigarrow$ 1 km costs 0.1€
1 hour costs 14.4€

Results (1)

Server-Metric: **Time-Dependent**

# route nodes	client metric	method	via nodes			time [ms]
			#	max.	rate[%]	
996	free flow	Dijkstra	0.071	3	0.006	1 500.78
		CH-based	0.068	3	0.006	0.36
	distance	Dijkstra	9.771	26	1.045	481.60
		CH-based	9.677	25	1.036	20.98
	energy	Dijkstra	1.103	6	0.125	1 326.17
		CH-based	1.094	6	0.124	1.72

- Fast with CH: less than 21 ms
- Slow with Dijkstra: up to 1.5 s
- Good compression: max 26 via nodes, avg < 10
- 2 bit/edge need \approx 248 byte, 10 via nodes need \approx 104 byte

Results (2)

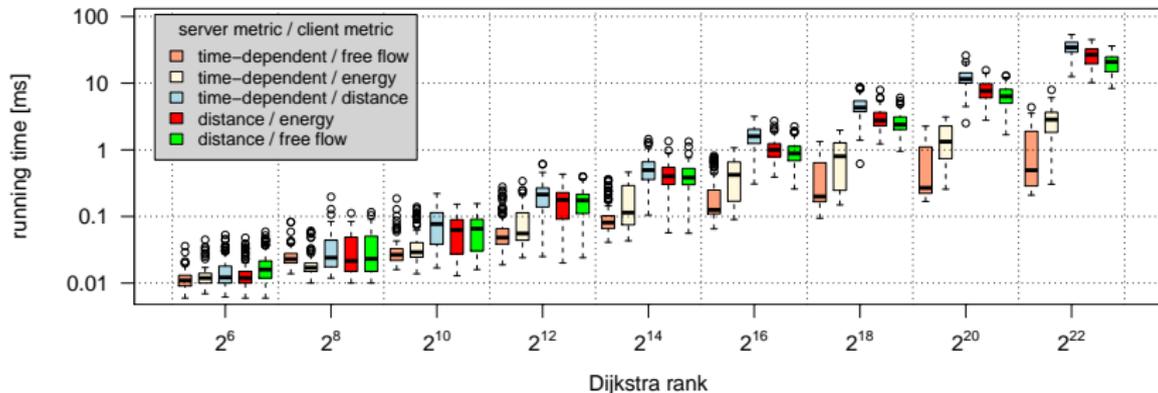
Server-Metric: **Distance**

# route nodes	client metric	method	via nodes			time [ms]
			#	max.	rate[%]	
1 763	free flow	Dijkstra	29.312	76	1.689	162.49
		CH-based	29.284	76	1.688	12.56
	energy	Dijkstra	24.902	69	1.434	182.87
		CH-based	24.876	69	1.433	15.63

- **Fast** with **CH**: less than **16 ms**
- **Slow** with **Dijkstra**: up to **183 ms**
- Still **good** compression: max **76** via nodes, avg **< 30**
- **Dijkstra** faster with more via nodes

Results (3)

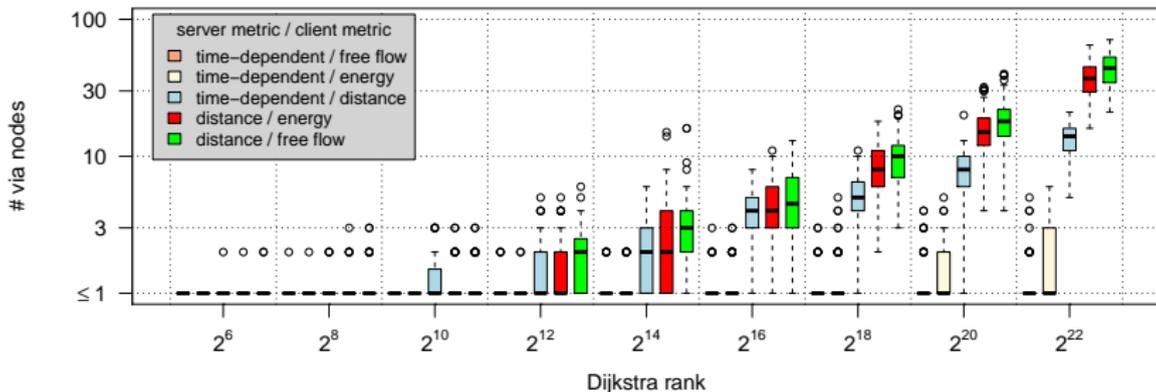
CH-Based: Running Time



- Running time **increases** with route length
- Even longest routes < 100 ms
- Ranks $2^{12} - 2^{14}$: middle sized German town, mostly < 1 ms

Results (4)

CH-Based: # Via Nodes



- # via nodes increases with route length
- There are outliers, but not serious
- Running time roughly increases with via nodes...
... remember $O(\log |P| \cdot \# \text{ via nodes})$ bidir. searches

Experimental results:

- Fast (de)compression with CH: $< 100 \text{ ms} + 21 \text{ ms}$
- Few via nodes: avg ≤ 30 , max 76
- Compression with CH practically not better

Convenience of use:

- Driver experiences no delay...
- ...except for latency of mobile radio network

- Speedup **Dijkstra-based** compression (use **ALT** or **ArcFlags**)
- **Faster** CH-based without repeated **bidir.** searches?
- **Non-pessimistic** CH-based **better?**

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Questions?